

# Language Modeling for Optimization

Yutian Chen, Richard Song


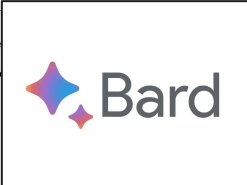
13 September 2023

## Attention Is All You Need

## Language Models are Few-Shot Learners

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rch  
com

Tom B. Brown\* Benjamin Mann\* Nick Ryder\* Melanie Subbiah\*  
 Jared Kaplan<sup>1</sup> Prafulla Dhariwal Arvind Neelakantan Pranav Shyam Girish Sastry  
 Amanda Askell Sandhini Agarwal Ariel Herbert-  
 Daniel M. Zie  
 Eric Sigh  
 Jack Clark  
 dford  
 OpenAI  
 Abstract

## Zero-Shot Text-to-Image Generation

Aditya Ramesh<sup>1</sup> Mikhail Pavlov<sup>1</sup> Gabriel Goh<sup>1</sup> Scott Gray<sup>1</sup>  
 Chelsea Voss<sup>1</sup> Alec Radford<sup>1</sup> Mark Chen<sup>1</sup> Ilya Sutskever<sup>1</sup>

### Abstract

Text-to-image generation has traditionally fo-  
 cused on finding better training on a fixed da-  
 might involve compl-  
 losses, or side inform-  
 bels or segmentation r-  
 ing. We describe a sim-  
 based on a transforme-  
 els the text and image  
 data. With sufficient d-  
 is competitive with pre-  
 els when evaluated in



## AudioLM: a Language Modeling Approach to Audio Generation

Zalán Borsos, Raphaël Marinier, Damien Vincent, Eugene Khartikov, Olivier Pietquin,  
 Matt Sharif, Dominik Roblek, Olivier Teboul, David Grangier, Marco Tagliasacchi, Neil Zeghidour

Abstract—We introduce AudioLM, a framework for high-quality audio generation with long-term consistency. AudioLM maps the input audio to a sequence of discrete tokens and casts au-

relying on textual annotations. Yet, the acoustic diversity and the quality remain limited: the model is trained on clean speech, and synthesis is restricted to a single speaker.



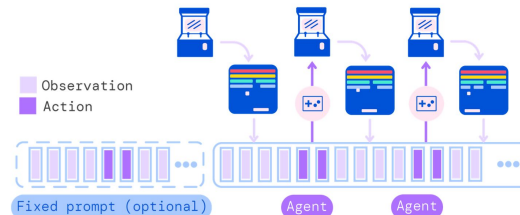
## A Generalist Agent

Scott Reed<sup>1</sup>, Konrad Żołna<sup>1</sup>, Emilio Parisotto<sup>1</sup>, Sergio Gómez Colmenarejo<sup>1</sup>, Alexander Novikov,  
 Gabriel Barth-Maron, Mai Giménez, Yury Sulsky, Jackie Kay, Jost Tobias Springenberg, Tom Eccles,  
 Jake Bruce, Ali Razavi, Ashley Edwards, Nicolas Heess, Yutian Chen, Raia Hadsell, Oriol Vinyals,  
 Mahyar Bordbar and Nando de Freitas<sup>1</sup>

<sup>1</sup>Equal contributions. All authors are affiliated with DeepMind

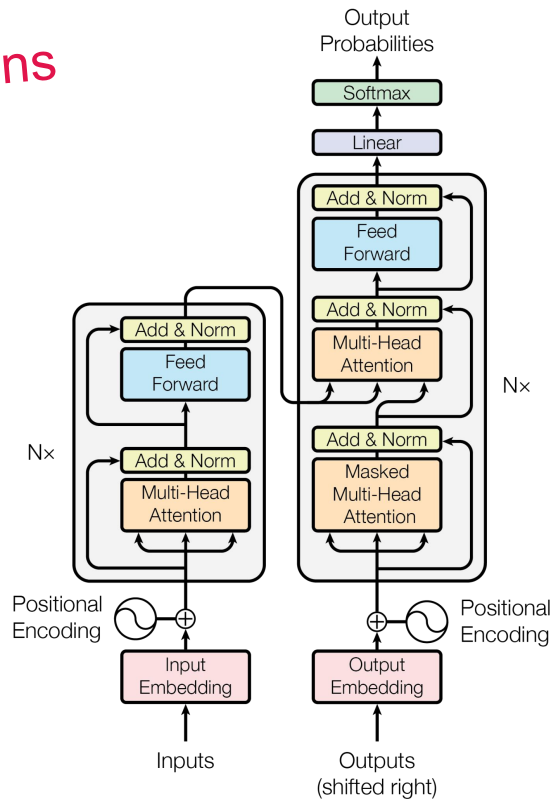
reedscot@deepmind.com

Reviewed on OpenReview: <https://openreview.net/forum?id=11k0k8jvj>

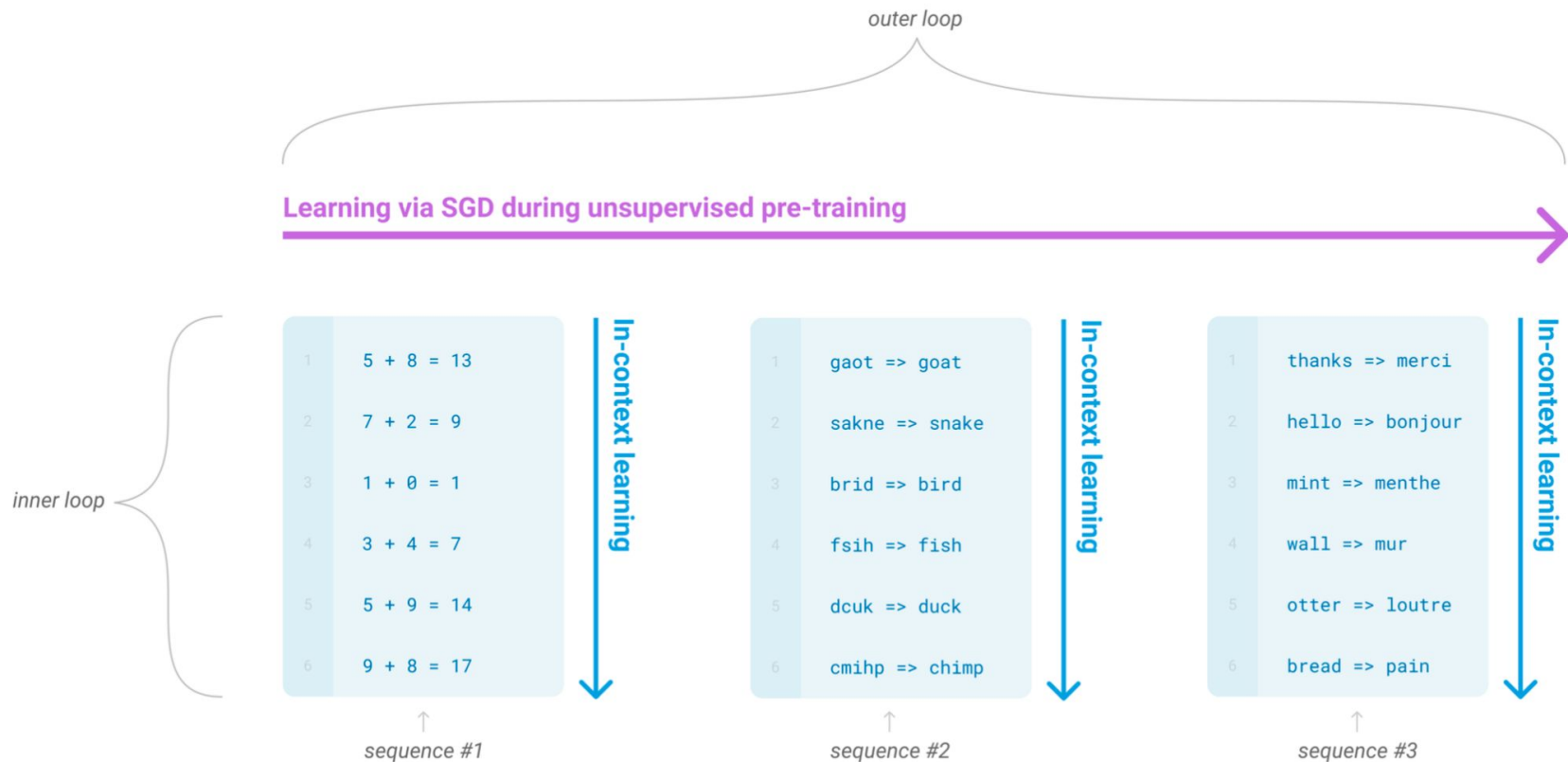


# Transformers (Vaswani et al., 2017)

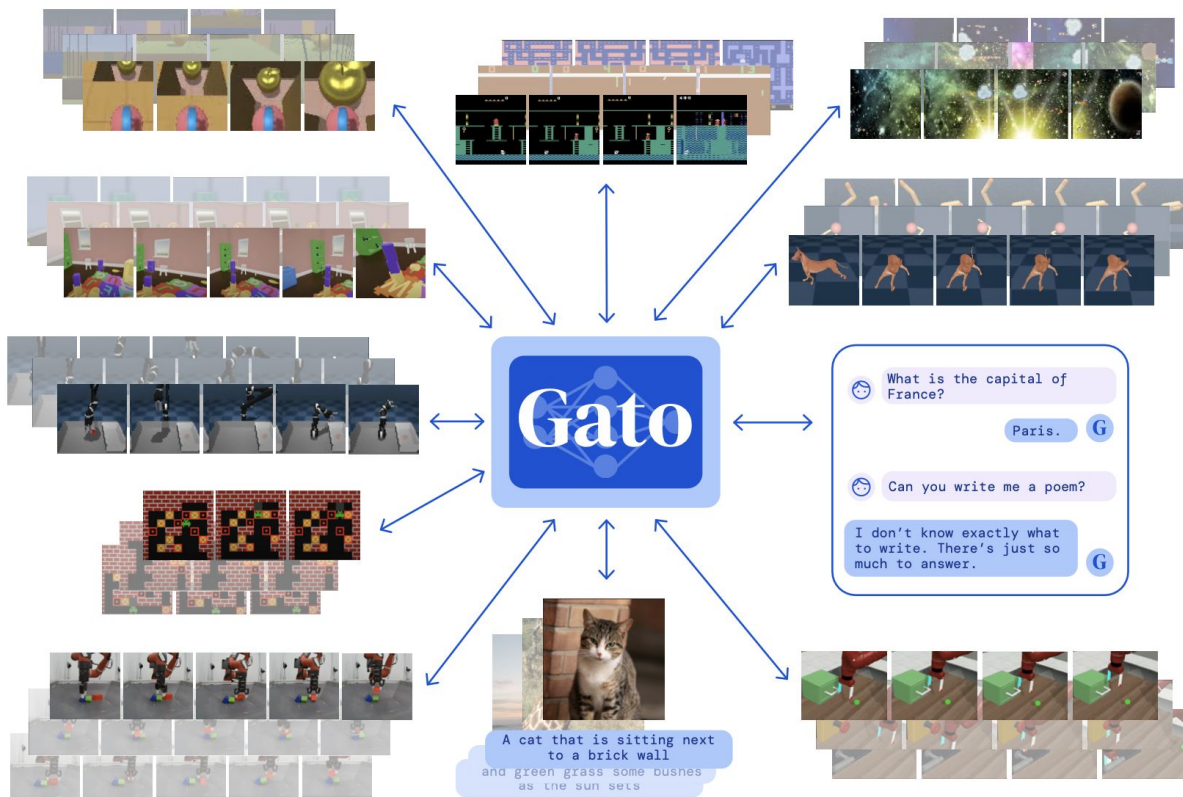
88K+ citations



# In-context learning



# Unifying multi-modality as a single language model



LLMs



- NLP
- Speech
- Vision
- Games
- Controls
- Robotics
- AI for Science
- ...
- AutoML

# AutoML

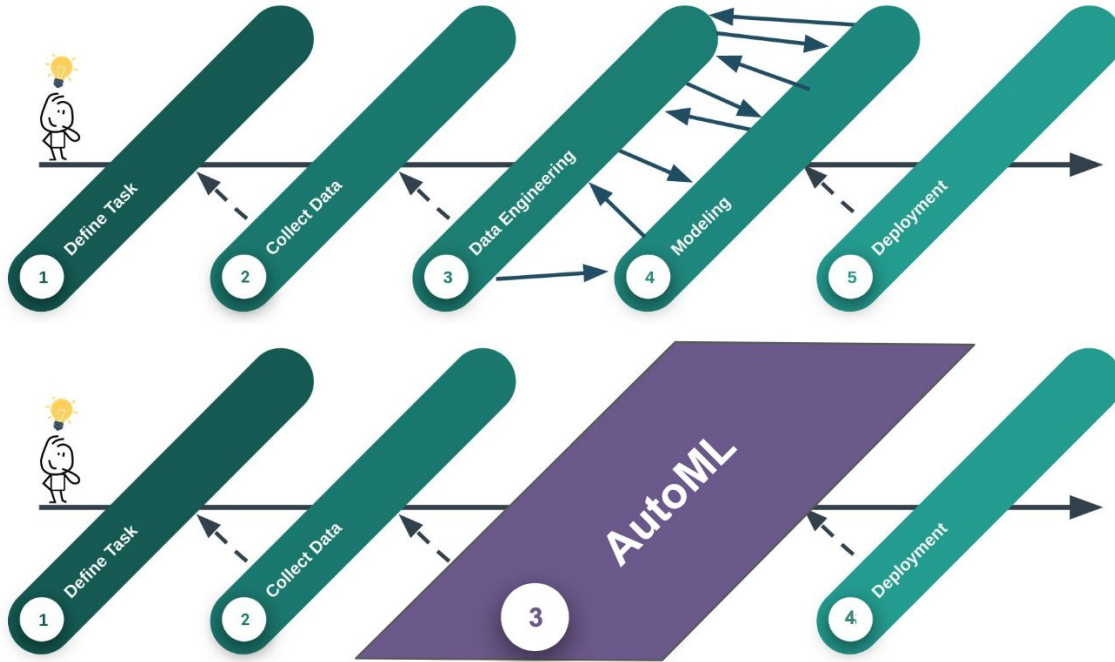
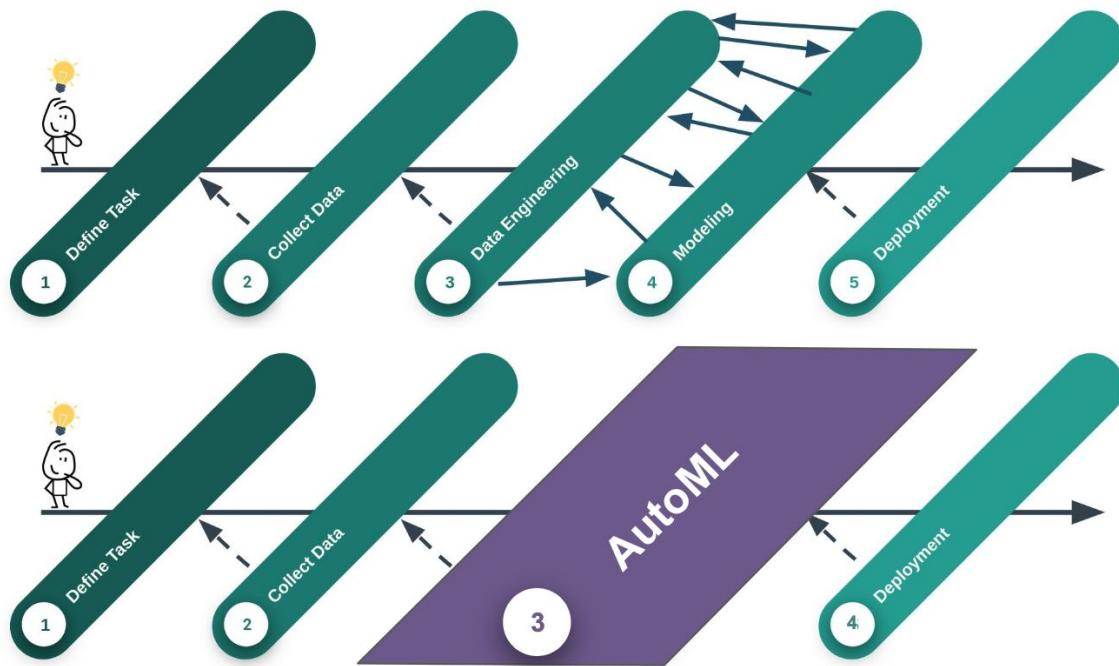


Figure source: <https://www.automl.org/talks/>

# AutoML

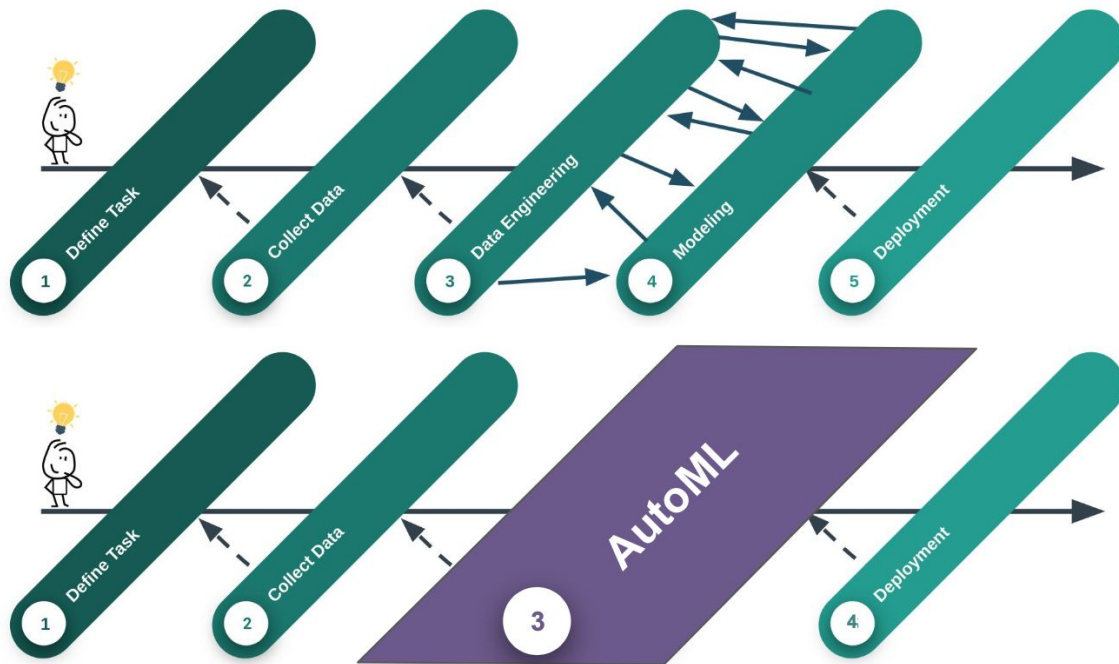


## **Traditional ML pipeline**

- *Data preprocess pipeline*
- *Feature engineering*
- *Select a model family*
- *Hyperparameters selection*
- *Model training*
- *Evaluation*



# AutoML



## **AutoML**

- *Hyperparameter optimization (HPO)*
- *Neural Architecture Search (NAS)*
- *Meta-learning*
- ...

# Optimization in AutoML

$$\lambda^* = \arg \min_{\lambda \in \Lambda} \mathcal{L}(\lambda, \mathcal{D}_{\text{train}}, \mathcal{D}_{\text{valid}})$$

- Hyperparameter optimization (HPO)
  - $\lambda$ : hyperparameter values
- Neural Architecture Search (NAS)
  - $\lambda$ : network architecture
- Meta-learning
  - $\lambda$ : optimization algorithm, model initialization, etc
- ...

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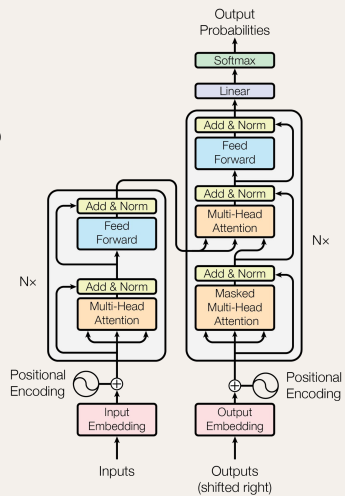
## ***Gradient-free optimization*** ***Black-box optimization (BBO)***

- *Bayesian optimization*
- *Reinforcement learning*
- *Evolutionary strategy*
- *Genetic algorithms*
- ...

# What can LMs do for AutoML?

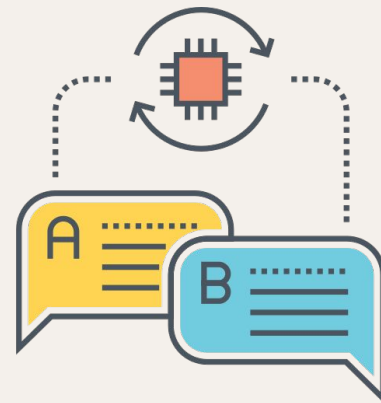
## Transformer architecture

- *Powerful modeling capacity*
- *In-context learning*



## Go beyond BBO

- *Leverage textual information*
- *More natural interface for AutoML*



# Outline

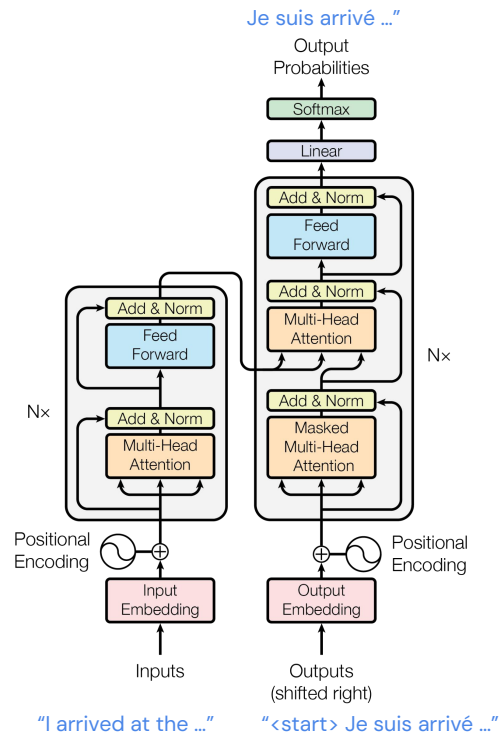
- Basics of language modeling and transformers
- Transformers for optimization
- Large language models for optimization
- Vision and opening questions

# Outline

- Basics of language modeling and transformers
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# The Transformer: Attention is all you need (Vaswani et al., 2017)

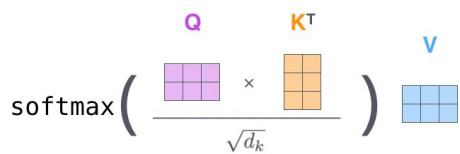
- Encoder-decoder architecture



# The Transformer: Attention is all you need (Vaswani et al., 2017)

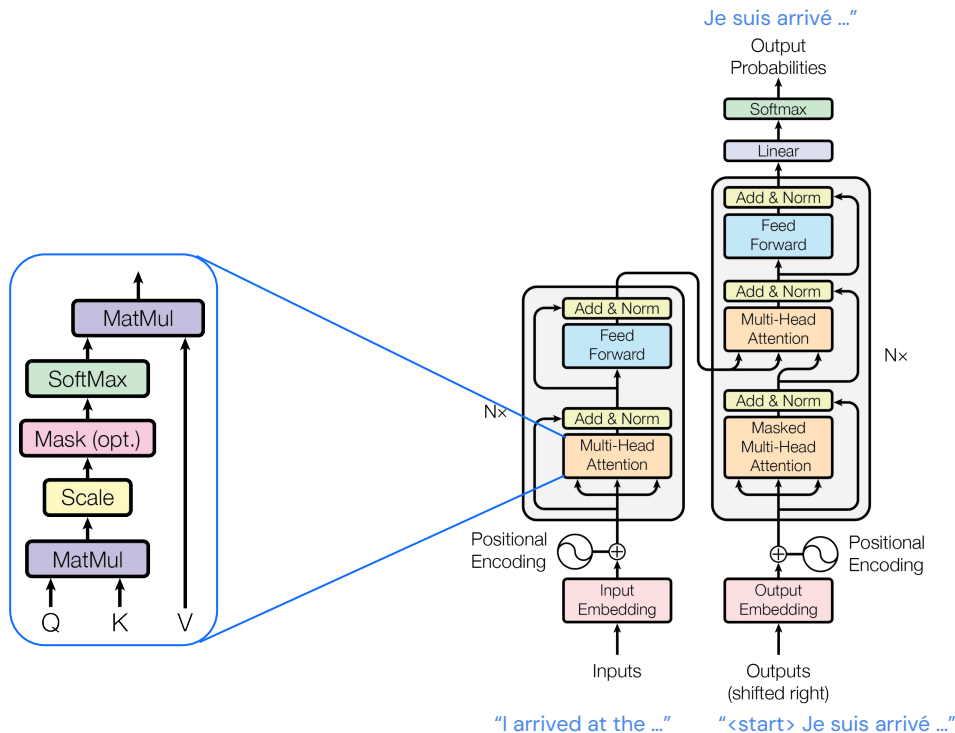
- Encoder-decoder architecture
- Attention-base sequence model
  - Scaled Dot-Product Attention

$$\text{Attention}(Q, K, V) = \text{softmax}\left(\frac{QK^T}{\sqrt{d_k}}\right)V$$



$$= Z$$

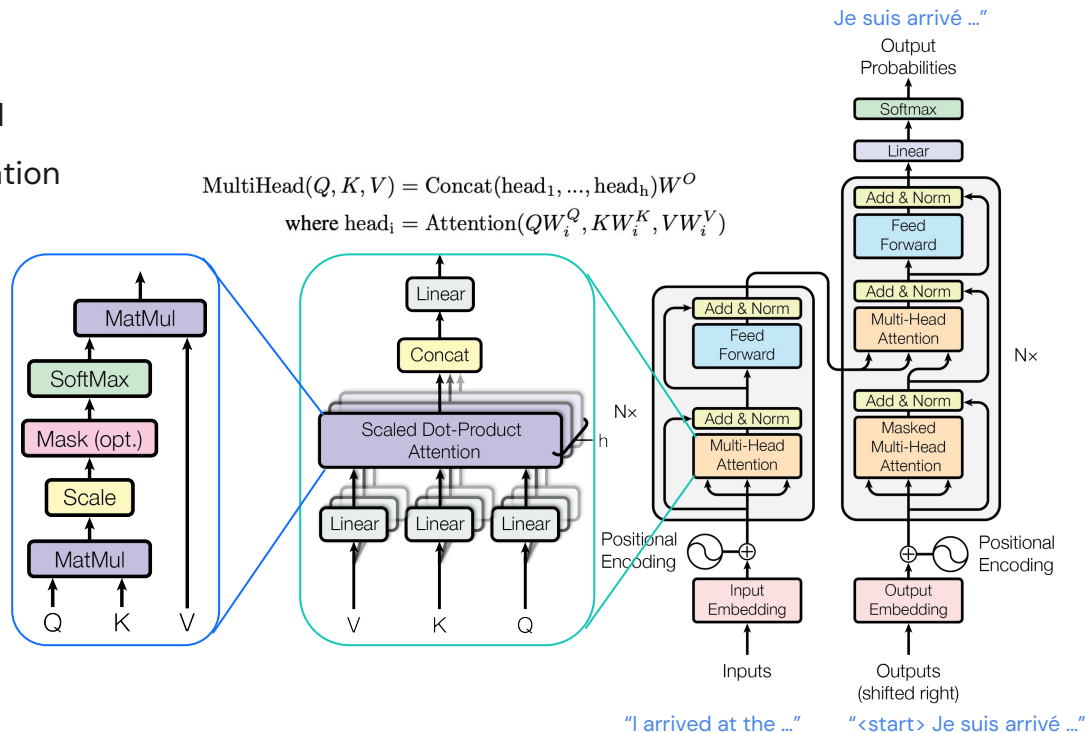
(Figure source: [jalanmar.github.io/illustrated-transformer](https://github.com/jalanmar/illustrated-transformer))





# The Transformer: Attention is all you need (Vaswani et al., 2017)

- Encoder-decoder architecture
- Attention-base sequence model
  - Scaled Dot-Product Attention
  - Multi-Head Attention

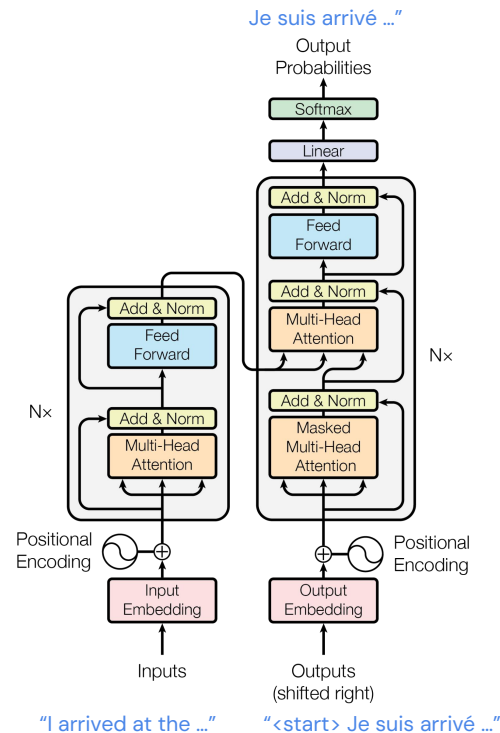
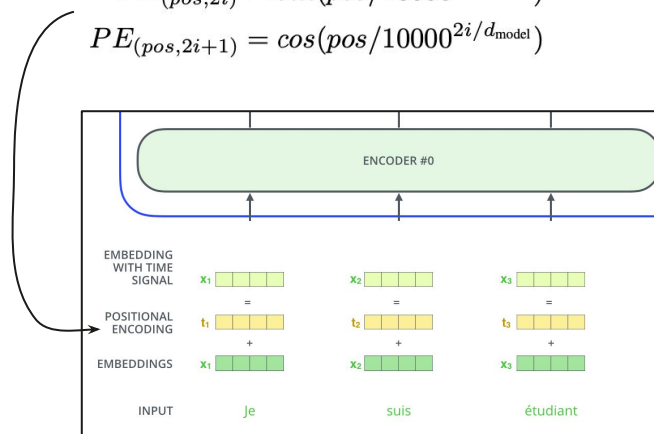


# The Transformer: Attention is all you need (Vaswani et al., 2017)

- Encoder-decoder architecture
- Attention-based sequence model
- Positional encoding - representing the order of the sequence

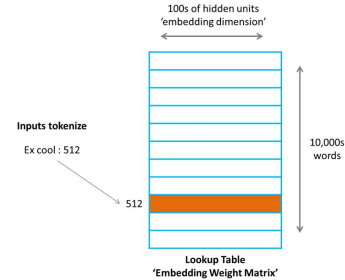
$$PE_{(pos,2i)} = \sin(pos/10000^{2i/d_{model}})$$

$$PE_{(pos,2i+1)} = \cos(pos/10000^{2i/d_{model}})$$



# Transformers inputs

- **Text**
  - Tokenizer: sentence  $\rightarrow$  token ids  
"I arrived at the ..."  $\rightarrow$  40, 5284, 379, 262, ...
  - Embedding table: token ids  $\rightarrow$  embedding vectors  
40, 5284, 379, 262, ...  $\rightarrow$  Inputs =  $[e_{40}, e_{5284}, e_{379}, e_{262}, \dots]$



# Transformers inputs

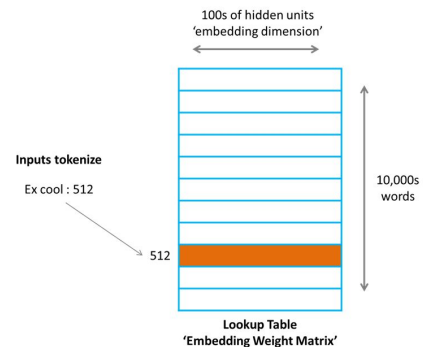
- **Text**

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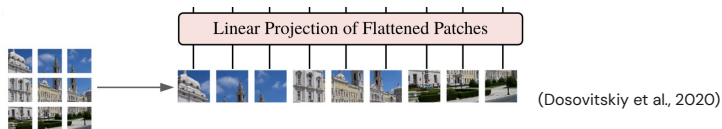
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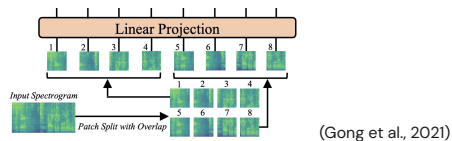
40, 5284, 379, 262, ...  $\rightarrow$  Inputs =  $[e_{40}, e_{5284}, e_{379}, e_{262}, \dots]$



- **Images**



- **Audio**



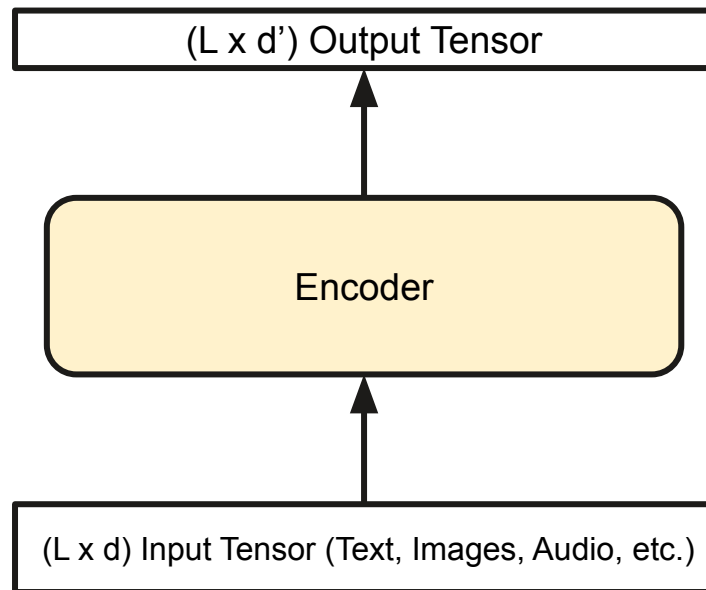
- **Discrete features**: One-hot encoding

**Continuous features**: Normalization (linear, mu-law, Riemann distribution)

# Transformers outputs: representation learning

## Use raw output ( $L \times d'$ ) in any way

- Directly into downstream models
- Take single slice (e.g. embeddings)

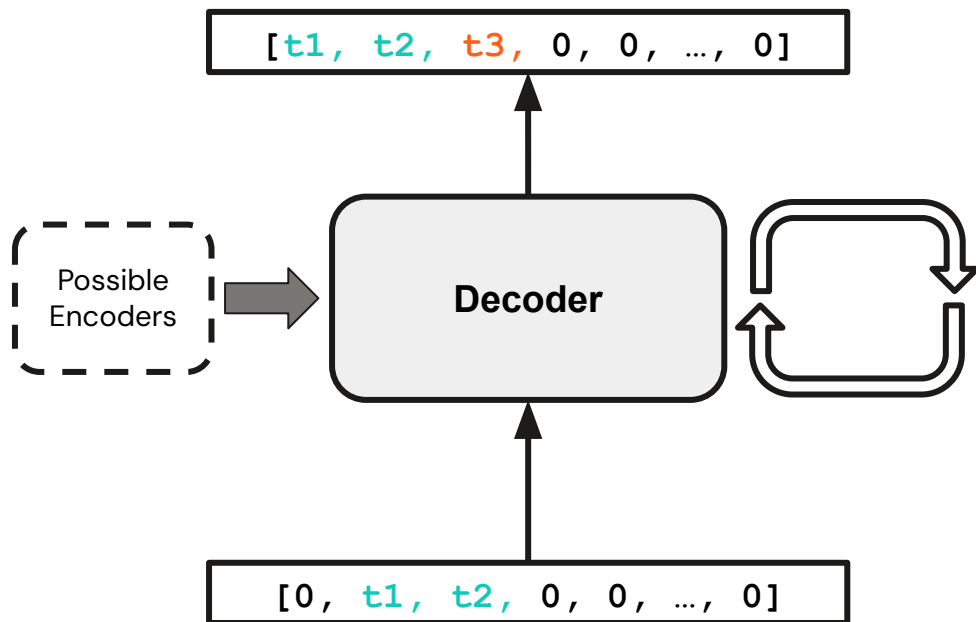


# Transformers outputs: answer generation

**Multi-step decoding:** 1 forward pass = **1 new token**

## Decoding Methods

- Ancestral Sampling
  - Temperature sampling
  - Top-K Sampling
  - Nucleus Sampling
  - ...
- Max likelihood sequence
  - Beam Search

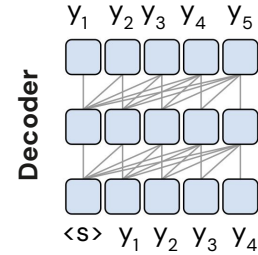


# Transformers pre-training

- **Causal language modeling** (e.g. GPT, PaLM)

$$\mathcal{L} = \sum_i \log P(y_i | \text{Decoder}(\mathbf{y}_{1:i-1}))$$

- E.g.  $\log P(\text{"Thank you for inviting me to your party last week"})$

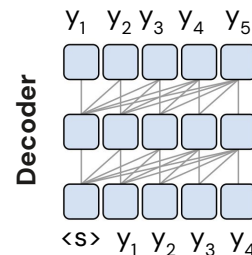


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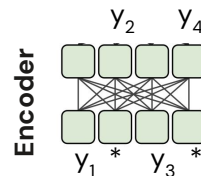
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- **Masked language modeling** (e.g. BERT (Kenton and Toutanova, 2019))

$$\mathcal{L} = \sum_{i \in \text{masked set}} \log P(y_i | \text{Encoder}(\mathbf{y}_{\text{masked}}))$$

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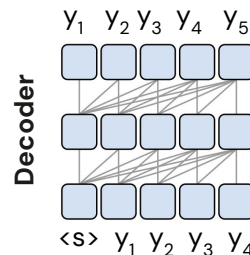


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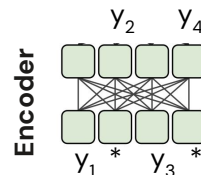
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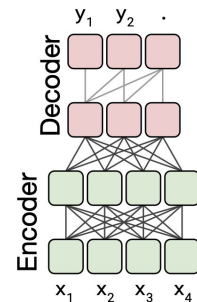
- E.g.  $\log P(\text{"* * * for inviting * * * * last *"} | \text{"Thank you * * me to your party * week"})$



- **Hybrid objective** (e.g. T5 (Raffel et al., 2020))

$$\mathcal{L} = \sum_i \log P(y_i | \text{Decoder}(\text{Encoder}(\mathbf{x}), \mathbf{y}_{1:i-1}))$$

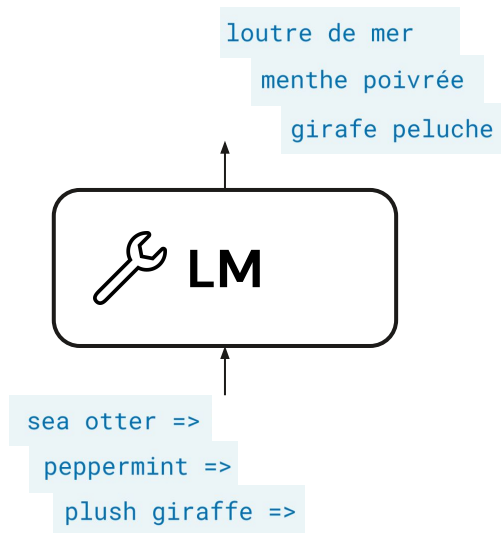
- E.g.  $\log P(\text{"<X> for inviting <Y> last"} | \text{"Thank you <X> me to your party <Y> week"})$



# Downstream applications

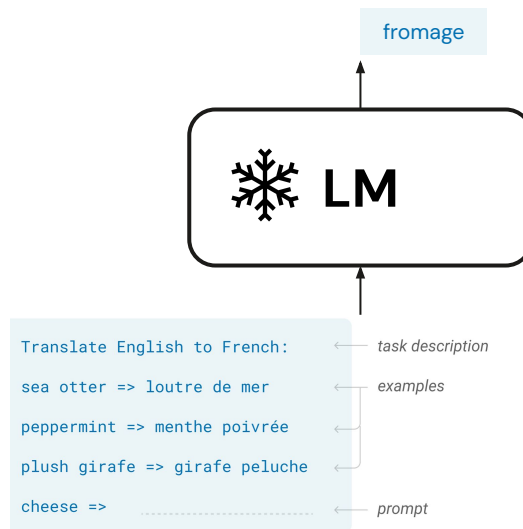
- **Fine-tuning**

- Fine-tuning parameters on new data
- Supervised FT
- Reinforcement learning FT (RLHF)



- **Prompting**

- Give task description and new data as **context** in the input



# Outline

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- **Transformers for optimization**
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# Optimization in AutoML

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- Hyperparameter optimization
  - $\lambda$ : hyperparameter values
- Neural Architecture Search (NAS)
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  - $\lambda$ : optimization algorithm, model initialization, etc
- ...

## **Gradient-free optimization** **Black-box optimization (BBO)**

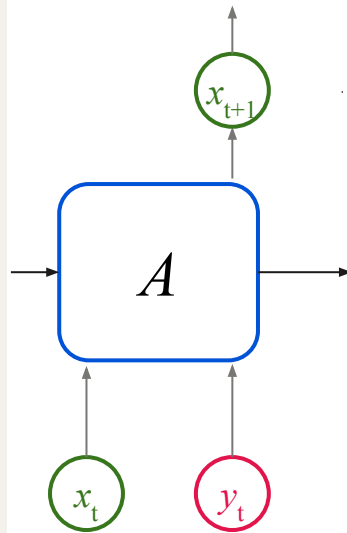
- *Bayesian optimization*
- *Reinforcement learning*
- *Evolutionary strategy*
- *Genetic algorithms*
- ...

# Iterative optimization as sequence modeling

$$x^* = \arg \min_{x \in \mathcal{X}} f(x)$$

- An iterative optimizer

$$\mathcal{A} : x_t, f(x_t), h_t \rightarrow x_{t+1}$$

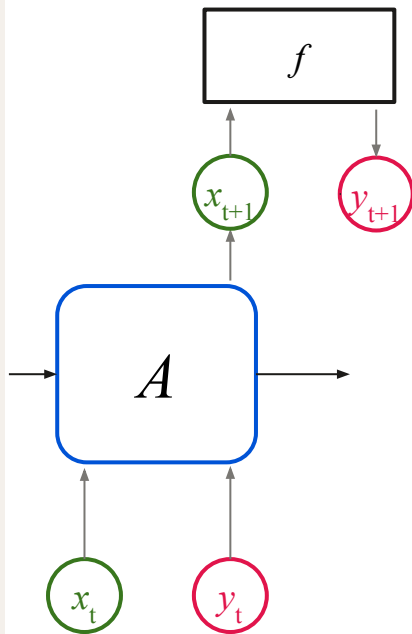


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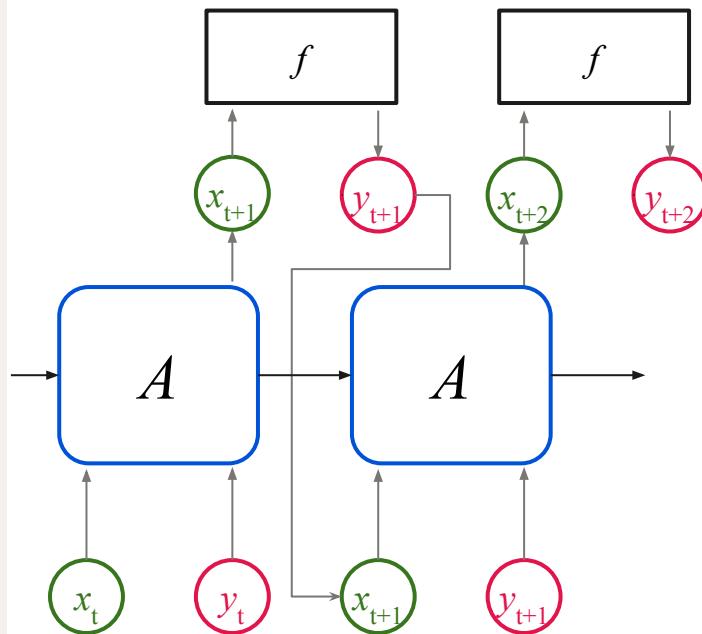


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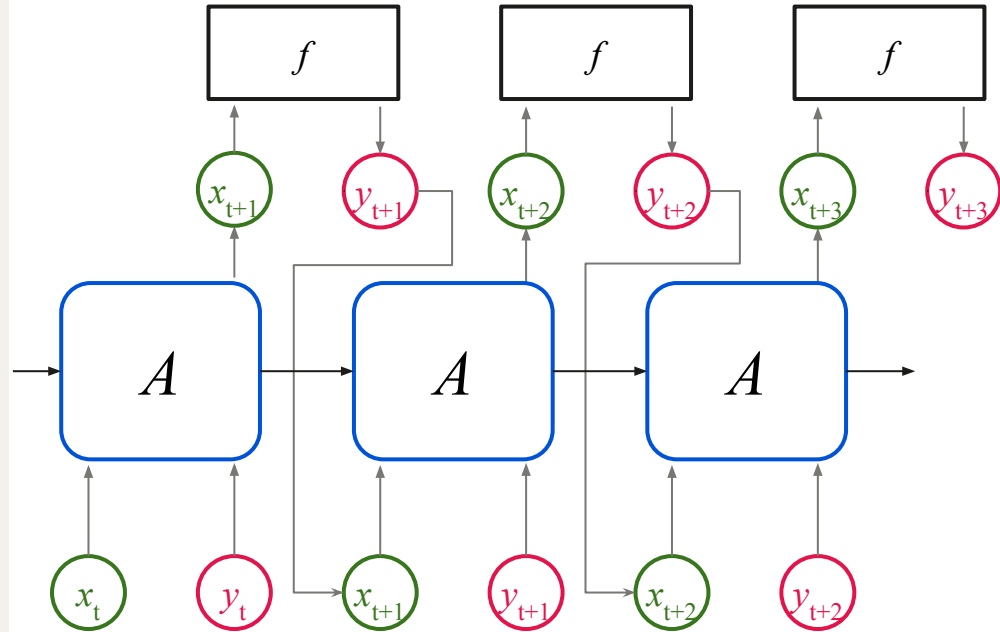


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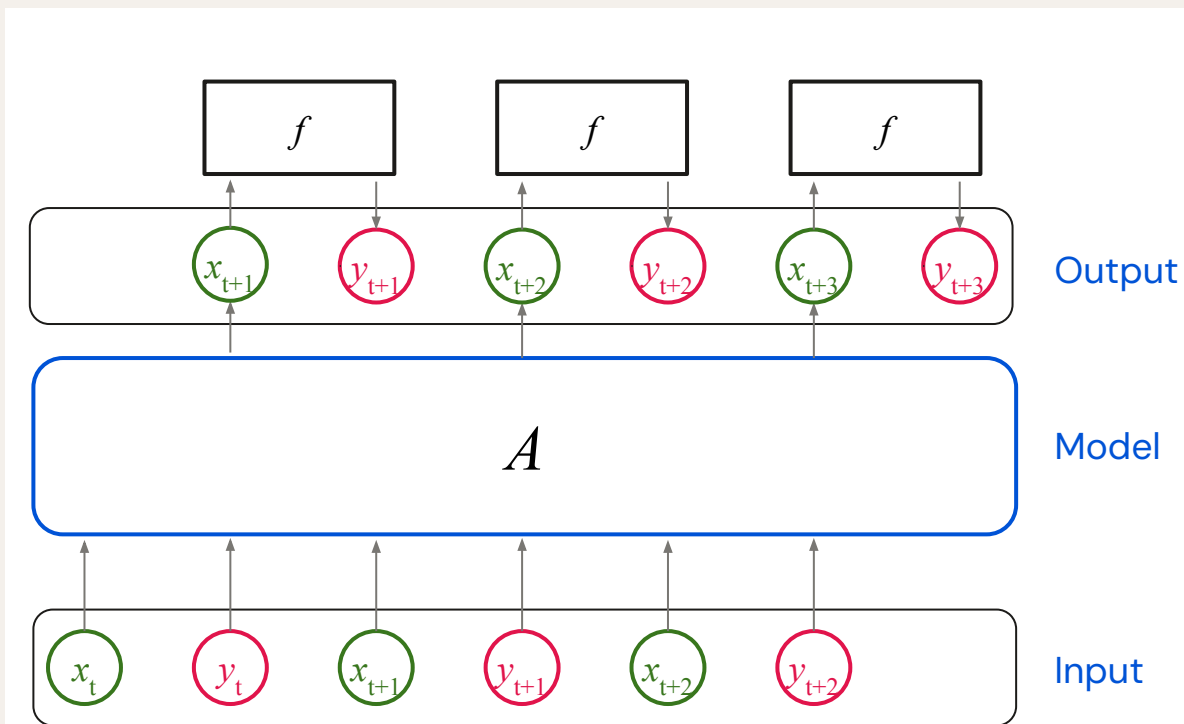
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$$\mathcal{A} : x_t, f(x_t), h_t \rightarrow x_{t+1}$$

- Sequence-input optimizer  
(Chen et al., 2017)

$$\mathcal{A} : \mathbf{x}_{1:t}, \mathbf{y}_{1:t} \rightarrow x_{t+1}$$



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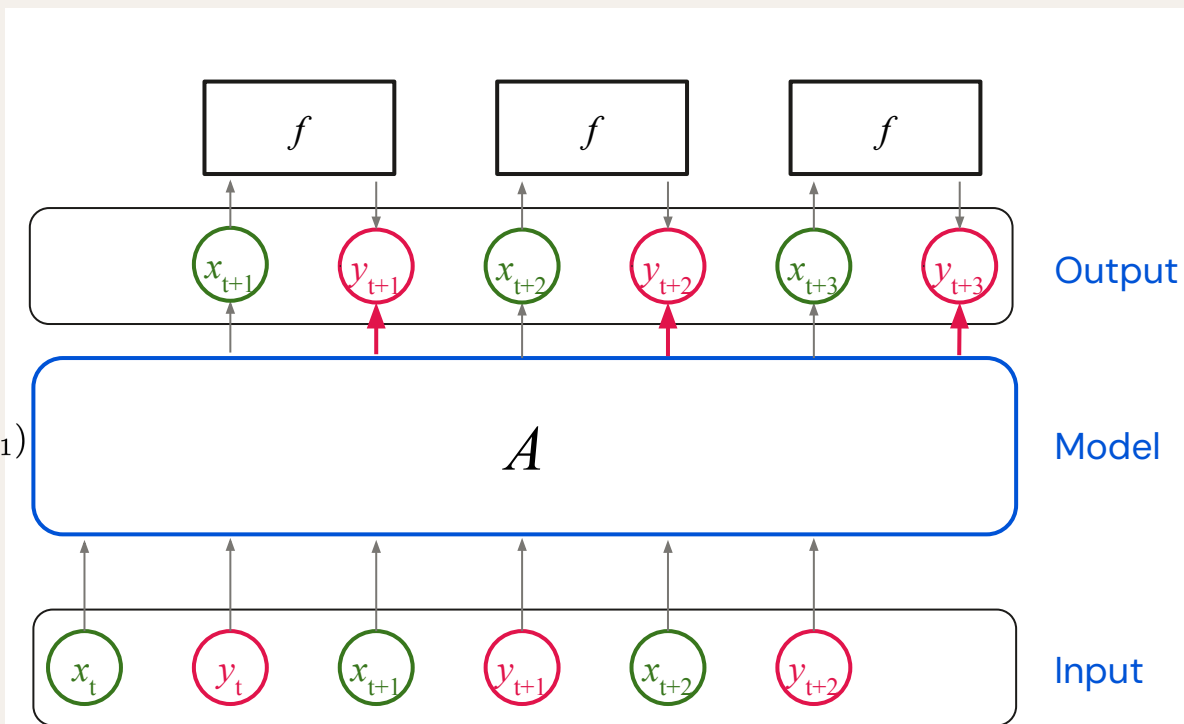
$$\mathcal{A} : x_t, f(x_t), h_t \rightarrow x_{t+1}$$

- Sequence-input optimizer  
(L2L (Chen et al., 2017))

$$\mathcal{A} : \mathbf{x}_{1:t}, \mathbf{y}_{1:t} \rightarrow x_{t+1}$$

- Function surrogate  $f_{\mathbf{x}_{1:t}, \mathbf{y}_{1:t}}(x_{t+1})$   
(Santoro et al., 2016)

$$\mathcal{A} : \mathbf{x}_{1:t}, \mathbf{y}_{1:t}, x_{t+1} \rightarrow y_{t+1}$$

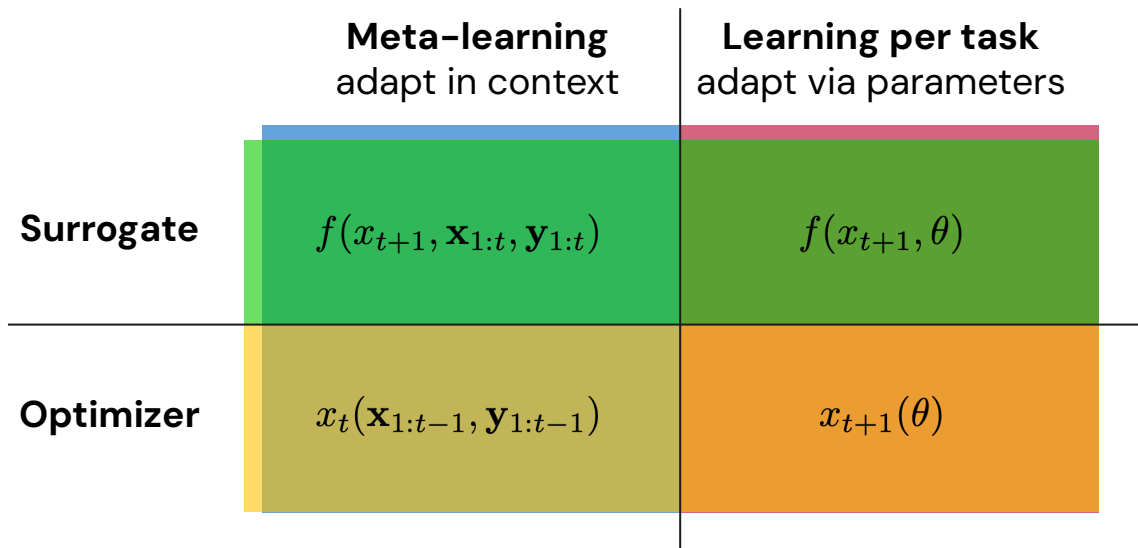


**Meta-learning**  
adapt in context

$$f(x_{t+1}, \mathbf{x}_{1:t}, \mathbf{y}_{1:t})$$

**Learning per task**  
adapt via parameters

$$f(x_{t+1}, \theta)$$

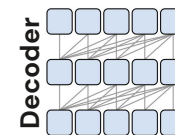
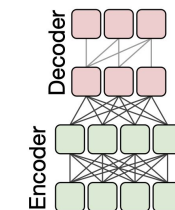
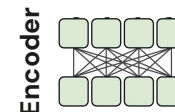


# Meta-learning surrogates

$$f(x_{t+1}, \mathbf{x}_{1:t}, \mathbf{y}_{1:t})$$

	Meta-learning adapt in context	Learning per task adapt via parameters
Surrogate	$f(x_{t+1}, \mathbf{x}_{1:t}, \mathbf{y}_{1:t})$	$f(x_{t+1}, \theta)$
Optimizer	$x_t(\mathbf{x}_{1:t-1}, \mathbf{y}_{1:t-1})$	$x_{t+1}(\theta)$

- *What's the input sequence (context)?*
- *How to encode the input?*
- **HPO surrogate**
  - $x_t$ : hyper-parameters,  $y_t$ : metric
  - **Context**: sequence of observations  $(x, y)_{1:t}$

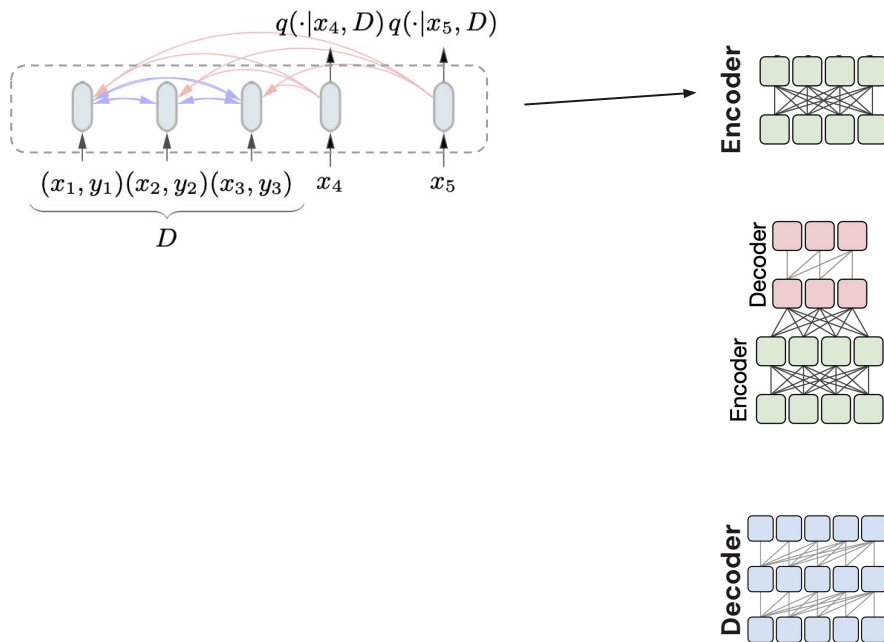


# Meta-learning surrogates

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- **How to encode the input?**
- **HPO surrogate**
  - $x_i$ : hyper-parameters,  $y_i$ : metric
  - **Context**: sequence of observations  $(x, y)_{1:t}$
  - PFNs (Muller et al., 2021; Muller et al., 2023)  
 $e_t = \text{Linear}(\mathbf{x}_t, y_t)$



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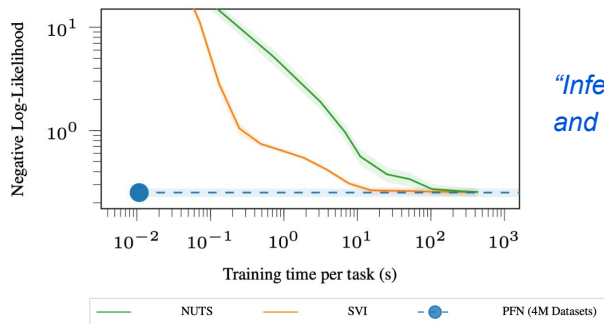
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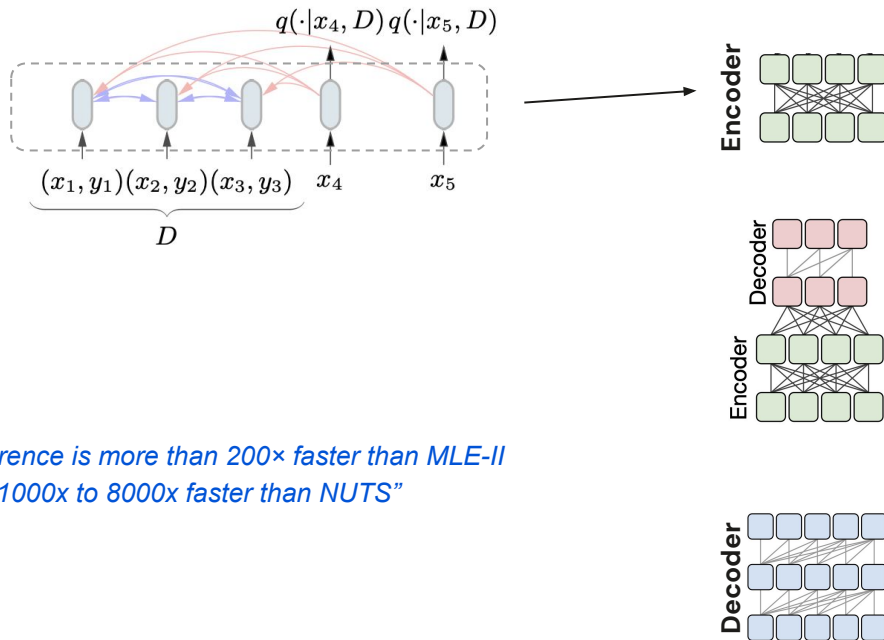
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$$e_t = \text{Linear}(\mathbf{x}_t, y_t)$$



*"Inference is more than 200x faster than MLE-II and 1000x to 8000x faster than NUTS"*



# Meta-learning surrogates

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	Meta-learning adapt in context	Learning per task adapt via parameters
Surrogate	$f(x_{t+1}, \mathbf{x}_{1:t}, \mathbf{y}_{1:t})$	$f(x_{t+1}, \theta)$
Optimizer	$x_t(\mathbf{x}_{1:t-1}, \mathbf{y}_{1:t-1})$	$x_{t+1}(\theta)$

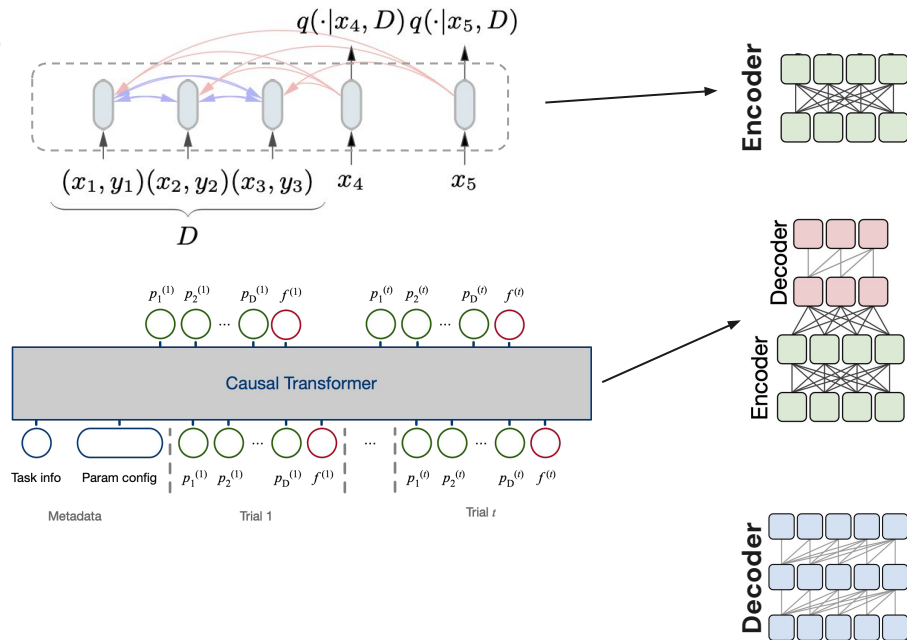
- **What's the input sequence (context)?**
- **How to encode the input?**

## • HPO surrogate

- $x_i$ : hyper-parameters,  $y_i$ : metric
- **Context**: sequence of observations  $(x, y)_{1:t}$
- **PFNs** (Muller et al., 2021; Muller et al., 2023)
- **OptFormer** (Chen et al., 2022)

$$e_t = \text{Linear}(\mathbf{x}_t, \mathbf{y}_t)$$

$$e_t = [\text{Emb}_{x_t^1}, \dots, \text{Emb}_{x_t^D}, \text{Emb}_{y_t}]$$





# Meta-learning surrogates

$$f(x_{t+1}, \mathbf{x}_{1:t}, \mathbf{y}_{1:t})$$

	Meta-learning adapt in context	Learning per task adapt via parameters
Surrogate	$f(x_{t+1}, \mathbf{x}_{1:t}, \mathbf{y}_{1:t})$	$f(x_{t+1}, \theta)$
Optimizer	$x_t(\mathbf{x}_{1:t-1}, \mathbf{y}_{1:t-1})$	$x_{t+1}(\theta)$

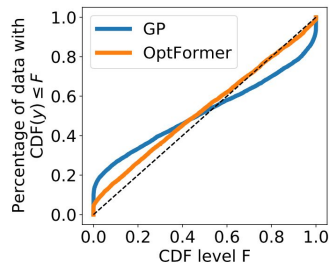
- **What's the input sequence (context)?**
- **How to encode the input?**

## • HPO surrogate

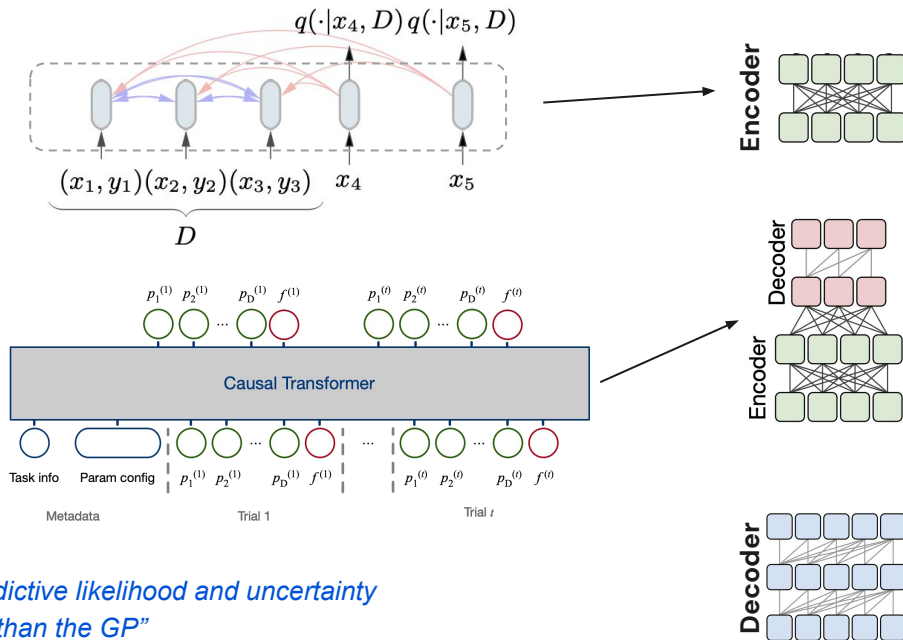
- $x_i$ : hyper-parameters,  $y_i$ : metric
- **Context**: sequence of observations  $(x, y)_{1:t}$
- **PFNs** (Muller et al., 2021; Muller et al., 2023)
- **OptFormer** (Chen et al., 2022)

$$e_t = \text{Linear}(\mathbf{x}_t, y_t)$$

$$e_t = [\text{Emb}_{x_1^1}, \dots, \text{Emb}_{x_t^D}, \text{Emb}_{y_t}]$$



*“Better predictive likelihood and uncertainty calibration than the GP”*



# Meta-learning surrogates

$$f(x_{t+1}, \mathbf{x}_{1:t}, \mathbf{y}_{1:t})$$

	Meta-learning adapt in context	Learning per task adapt via parameters
Surrogate	$f(x_{t+1}, \mathbf{x}_{1:t}, \mathbf{y}_{1:t})$	$f(x_{t+1}, \theta)$
Optimizer	$x_t(\mathbf{x}_{1:t-1}, \mathbf{y}_{1:t-1})$	$x_{t+1}(\theta)$

- **What's the input sequence (context)?**
- **How to encode the input?**

## • HPO surrogate

- $x_i$ : hyper-parameters,  $y_i$ : metric
- **Context**: sequence of observations  $(x, y)_{1:t}$
- **PFNs** (Muller et al., 2021; Muller et al., 2023)
- **OptFormer** (Chen et al., 2022)

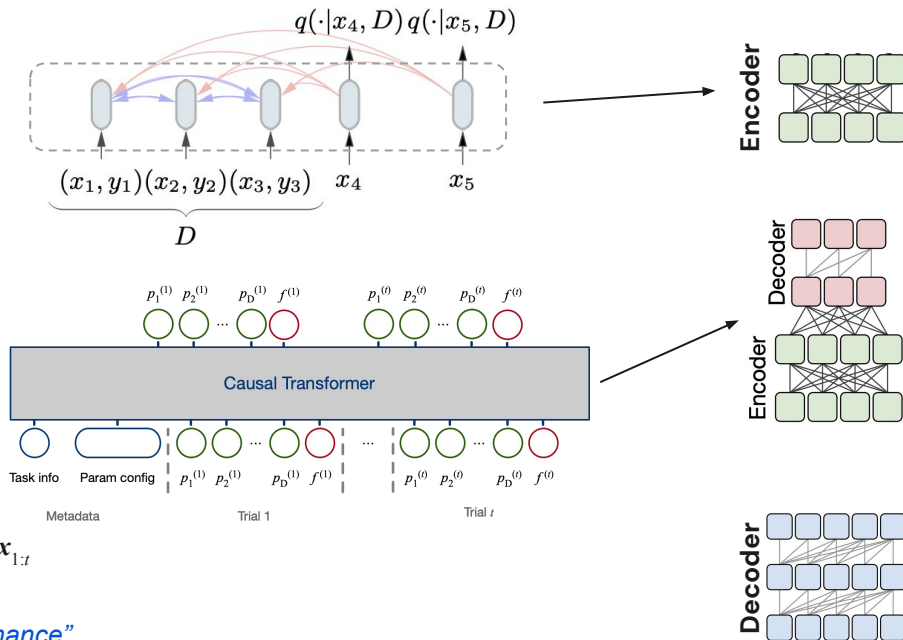
$$e_t = \text{Linear}(\mathbf{x}_t, y_t)$$

$$e_t = [\text{Emb}_{x_1^1}, \dots, \text{Emb}_{x_t^D}, \text{Emb}_{y_t}]$$

## • Tabular data

- **TabPFN** (Hollmann et al., 2022)
  - **Context**: sequence of data points in  $x_{1:t}$

*“yields a 230× speedup on CPU and a 5700× speedup using a GPU with comparable performance”*



# Meta-learning surrogates

$$f(x_{t+1}, \mathbf{x}_{1:t}, \mathbf{y}_{1:t})$$

	Meta-learning adapt in context	Learning per task adapt via parameters
Surrogate	$f(x_{t+1}, \mathbf{x}_{1:t}, \mathbf{y}_{1:t})$	$f(x_{t+1}, \theta)$
Optimizer	$x_t(\mathbf{x}_{1:t-1}, \mathbf{y}_{1:t-1})$	$x_{t+1}(\theta)$

- **What's the input sequence (context)?**
- **How to encode the input?**

## • HPO surrogate

- $x_t$ : hyper-parameters,  $y_t$ : metric
- **Context**: sequence of observations  $(x, y)_{1:t}$
- **PFNs** (Muller et al., 2021; Muller et al., 2023)
- **OptFormer** (Chen et al., 2022)

$$e_t = \text{Linear}(\mathbf{x}_t, y_t)$$

$$e_t = [\text{Emb}_{x_t^1}, \dots, \text{Emb}_{x_t^D}, \text{Emb}_{y_t}]$$

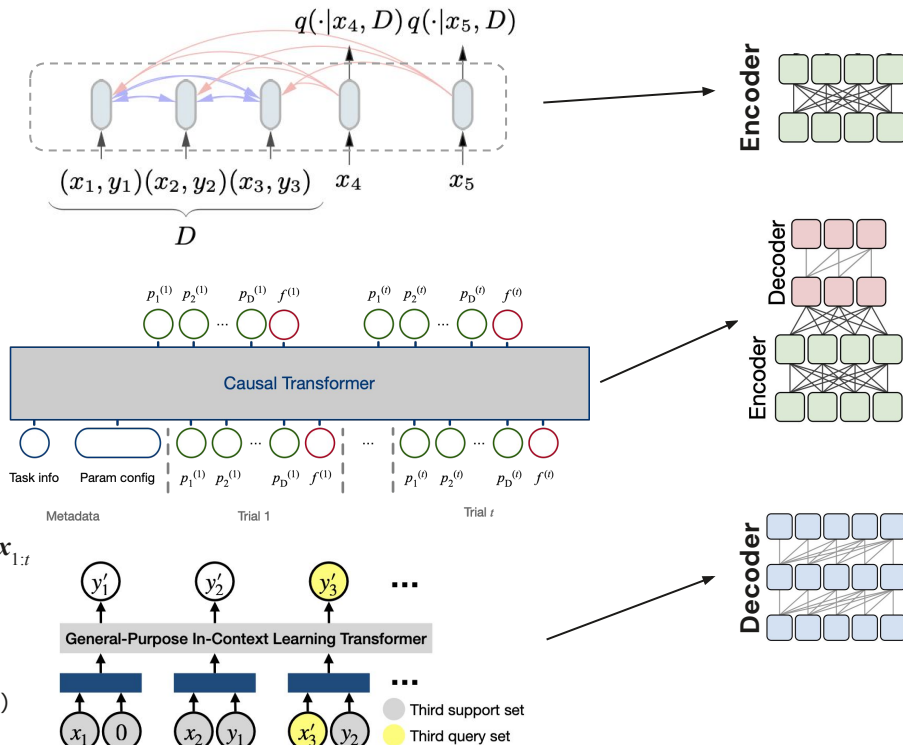
## • Tabular data

- **TabPFN** (Hollmann et al., 2022)
  - **Context**: sequence of data points in  $x_{1:t}$

## • Meta-learning

- **Context**: sequence of observations  $(x, y)_{1:t}$
- **GPICL** for image classification (Kirsch et al., 2022)

$$e_t = \text{MLP}(y_{t-1}, \mathbf{x}_t)$$



# Meta-learning surrogates

$$f(x_{t+1}, \mathbf{x}_{1:t}, \mathbf{y}_{1:t})$$

	Meta-learning adapt in context	Learning per task adapt via parameters
Surrogate	$f(x_{t+1}, \mathbf{x}_{1:t}, \mathbf{y}_{1:t})$	$f(x_{t+1}, \theta)$
Optimizer	$x_t(\mathbf{x}_{1:t-1}, \mathbf{y}_{1:t-1})$	$x_{t+1}(\theta)$

- **What's the input sequence (context)?**
- **How to encode the input?**

- **HPO surrogate**

- $x_t$ : hyper-parameters,  $y_t$ : metric
- **Context**: sequence of observations  $(x, y)_{1:t}$
- **PFNs** (Muller et al., 2021; Muller et al., 2023)
- **OptFormer** (Chen et al., 2022)

$$e_t = \text{Linear}(\mathbf{x}_t, y_t)$$

$$e_t = [\text{Emb}_{x_t^1}, \dots, \text{Emb}_{x_t^D}, \text{Emb}_{y_t}]$$

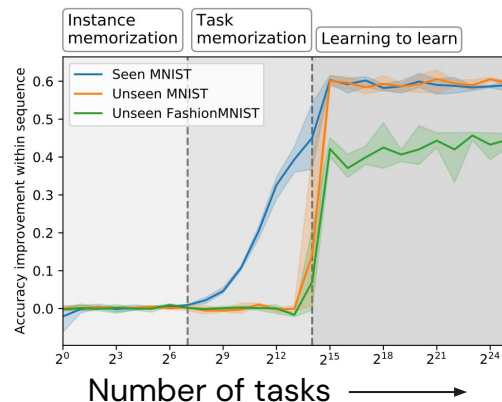
- **Tabular data**

- **TabPFN** (Hollmann et al., 2022)
  - **Context**: sequence of data points in  $x_{1:t}$

- **Meta-learning**

- **Context**: sequence of observations  $(x, y)_{1:t}$
- **GPICL** for image classification (Kirsch et al., 2022)

$$e_t = \text{MLP}(y_{t-1}, \mathbf{x}_t)$$



# Learning surrogates per task

$$f(x_{t+1}, \theta)$$

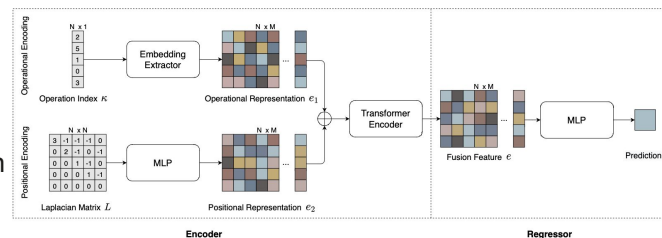
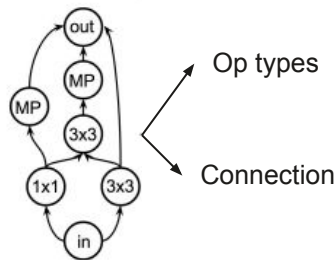
	Meta-learning adapt in context	Learning per task adapt via parameters
Surrogate	$f(x_{t+1}, x_{1:t}, y_{1:t})$	$f(x_{t+1}, \theta)$
Optimizer	$x_t(x_{1:t-1}, y_{1:t-1})$	$x_{t+1}(\theta)$

- **What's the input sequence (context)?**
- **How to encode the input?**

## • NAS predictor

- **Context:** nodes in an architecture  $x_{1:N}$
- TNASP (Lu et al., 2021)

$$e_n = \text{Emb}_{\text{Op}_n} + \text{MLP}(L)_n$$



# Learning surrogates per task

$$f(x_{t+1}, \theta)$$

	Meta-learning adapt in context	Learning per task adapt via parameters
Surrogate	$f(x_{t+1}, x_{1:t}, y_{1:t})$	$f(x_{t+1}, \theta)$
Optimizer	$x_t(x_{1:t-1}, y_{1:t-1})$	$x_{t+1}(\theta)$

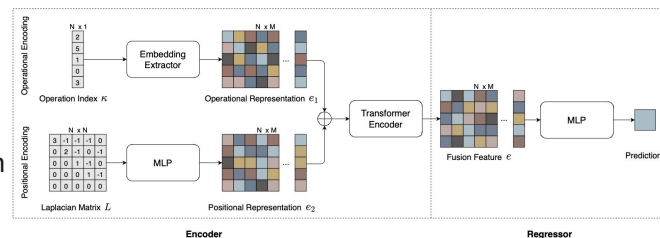
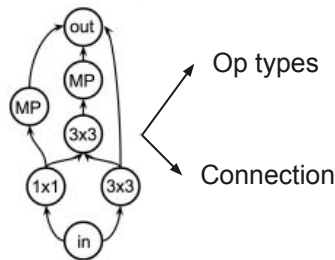
- **What's the input sequence (context)?**
- **How to encode the input?**

## • NAS predictor

- **Context:** nodes in an architecture  $x_{1:N}$
- TNASP (Lu et al., 2021)

$$e_n = \text{Emb}_{\text{Op}_n} + \text{MLP}(L)_n$$

*“Rank 2nd among all teams in CVPR 2021 NAS Competition Track 2: Performance Prediction Track”*



# Learning surrogates per task

## $f(x_{t+1}, \theta)$

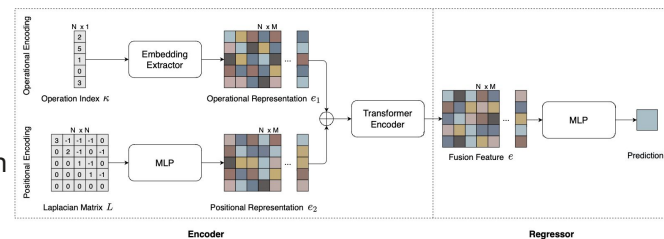
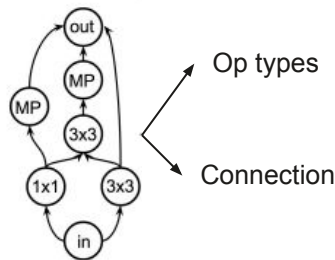
	Meta-learning adapt in context	Learning per task adapt via parameters
Surrogate	$f(x_{t+1}, x_{1:t}, y_{1:t})$	$f(x_{t+1}, \theta)$
Optimizer	$x_t(x_{1:t-1}, y_{1:t-1})$	$x_{t+1}(\theta)$

- **What's the input sequence (context)?**
- **How to encode the input?**

### • NAS predictor

- **Context:** nodes in an architecture  $x_{1:N}$
- **TNASP** (Lu et al., 2021)  

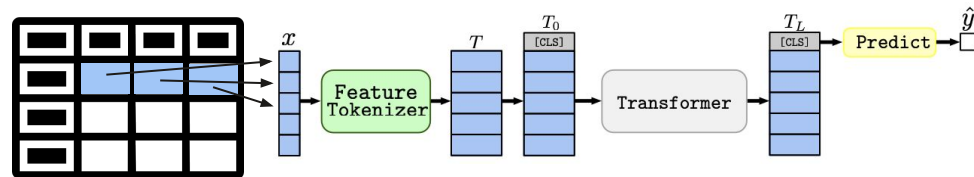
$$e_n = \text{Emb}_{\text{Op}_n} + \text{MLP}(L)_n$$



### • Tabular data

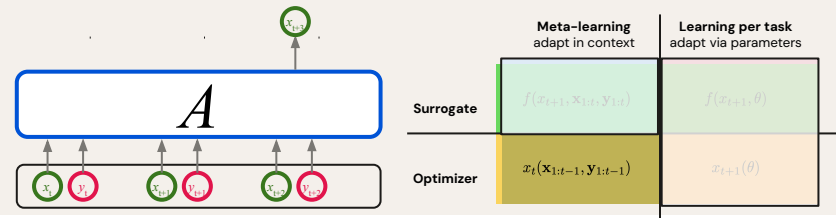
- **FT-Transformer** (Gorishniy et al., 2021)
  - **Context:** features in one observation in  $x_{1:D}$   

$$e_d = \text{Linear}(x_d)$$



# Meta-learning optimizer

$$x_t(\mathbf{x}_{1:t-1}, \mathbf{y}_{1:t-1})$$

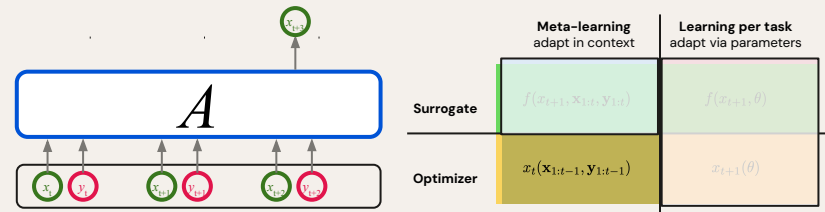


- *What's the input sequence (context)?*
- *How to encode the input?*



# Meta-learning optimizer

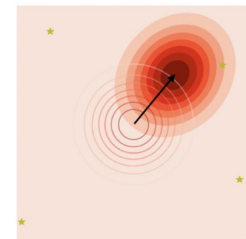
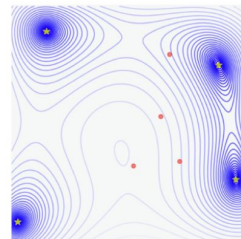
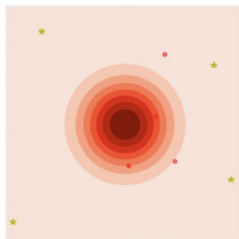
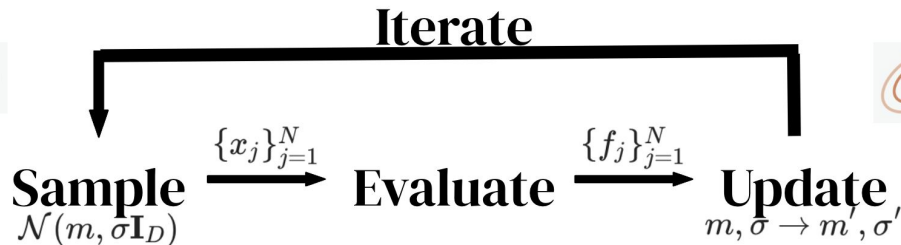
$$x_t(\mathbf{x}_{1:t-1}, \mathbf{y}_{1:t-1})$$



- *What's the input sequence (context)?*
- *How to encode the input?*

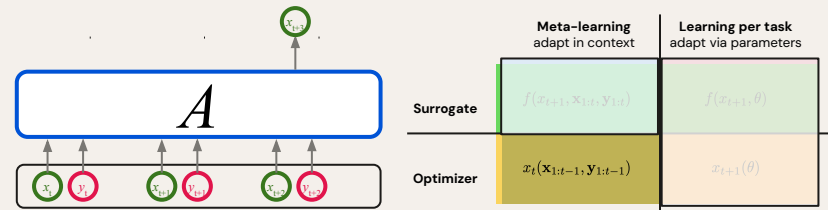
- **Population-based Optimizer**

- Evolutionary strategy (Lange et al., 2022)

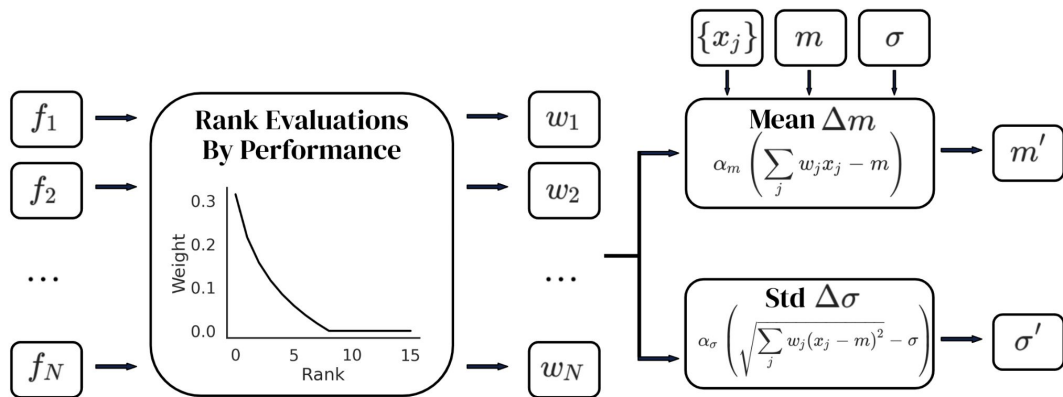


# Meta-learning optimizer

$$x_t(\mathbf{x}_{1:t-1}, \mathbf{y}_{1:t-1})$$

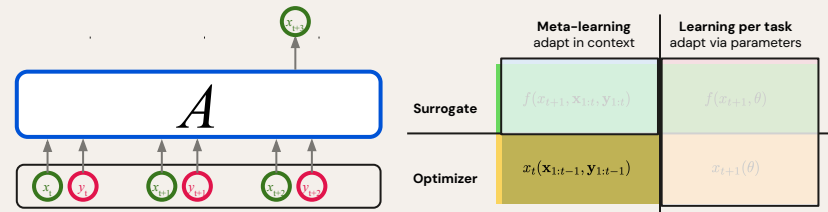


- *What's the input sequence (context)?*
- *How to encode the input?*
- **Population-based Optimizer**
  - Evolutionary strategy (Lange et al., 2022)

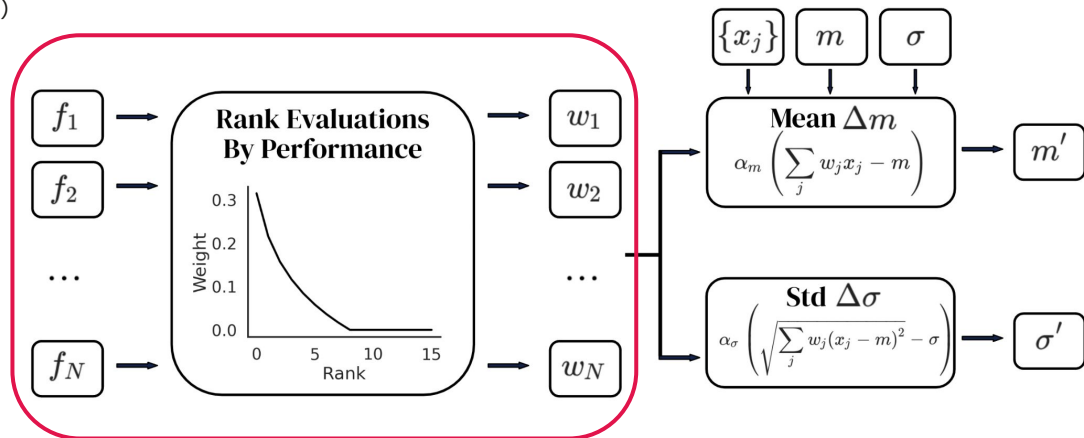


# Meta-learning optimizer

$$x_t(\mathbf{x}_{1:t-1}, \mathbf{y}_{1:t-1})$$

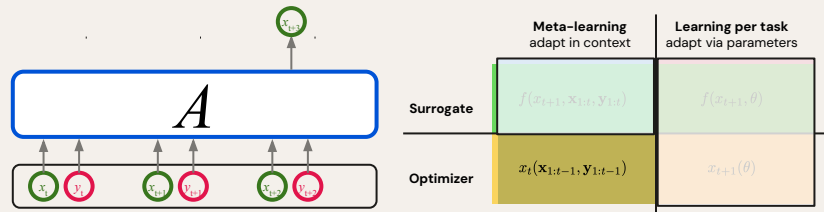


- *What's the input sequence (context)?*
- *How to encode the input?*
- **Population-based Optimizer**
  - Evolutionary strategy (Lange et al., 2022)



# Meta-learning optimizer

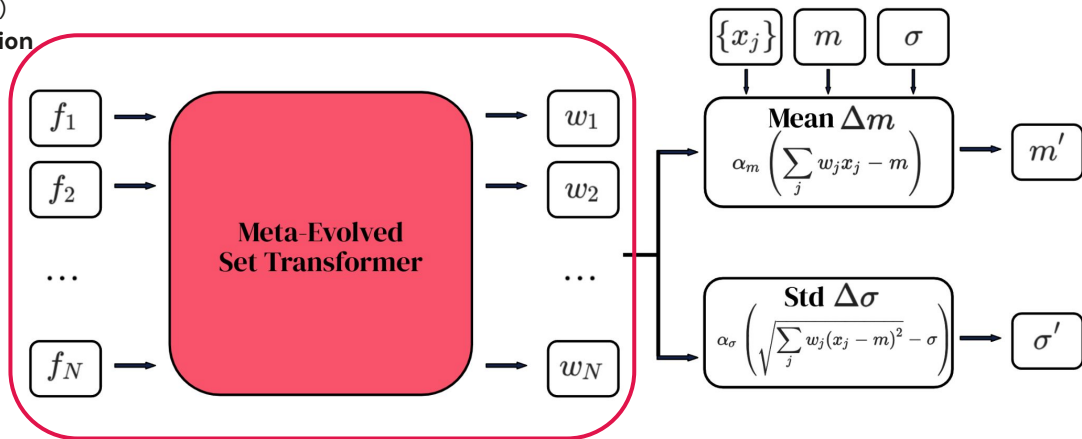
$$x_t(\mathbf{x}_{1:t-1}, \mathbf{y}_{1:t-1})$$



- **What's the input sequence (context)?**
- **How to encode the input?**

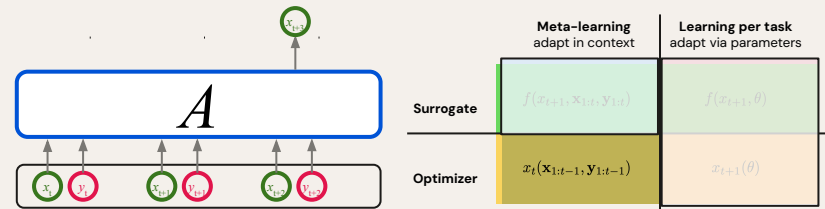
- **Population-based Optimizer**

- Evolutionary strategy (Lange et al., 2022)
  - **Context: population in a generation**  
 $(x_1, y_1), (x_2, y_2), \dots, (x_N, y_N)$   
 $w_1, \dots, w_N = \text{Transformer}(y_1, \dots, y_N)$



# Meta-learning optimizer

$$x_t(\mathbf{x}_{1:t-1}, \mathbf{y}_{1:t-1})$$



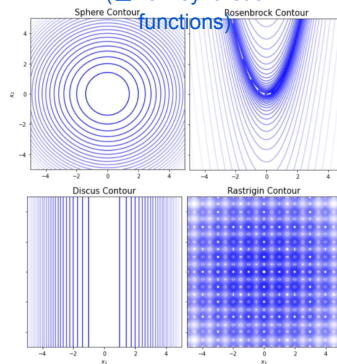
- **What's the input sequence (context)?**
- **How to encode the input?**

- **Population-based Optimizer**

- Evolutionary strategy (Lange et al., 2022)
  - **Context: population in a generation**  
 $(x_1, y_1), (x_2, y_2), \dots, (x_N, y_N)$   
 $w_1, \dots, w_N = \text{Transformer}(y_1, \dots, y_N)$

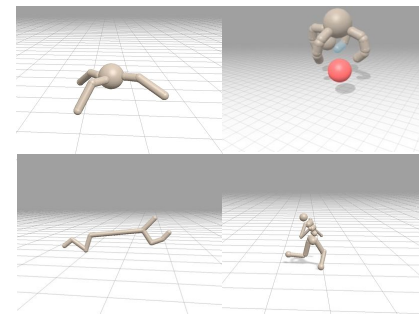
## Meta-train

( $\leq 10D$  synthetic functions)

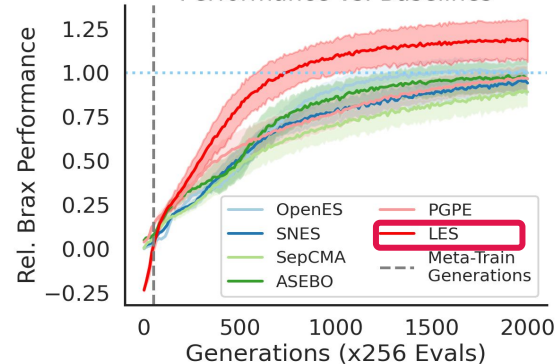


## Meta-test

(4-hidden layer MLP)

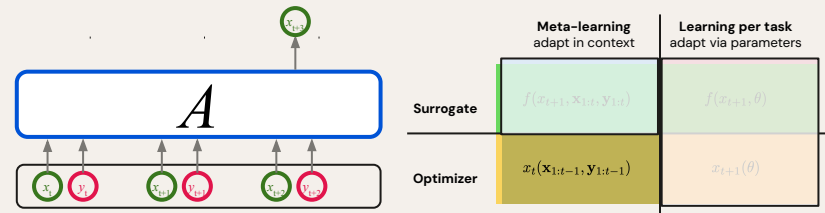


## Performance vs. Baselines



# Meta-learning optimizer

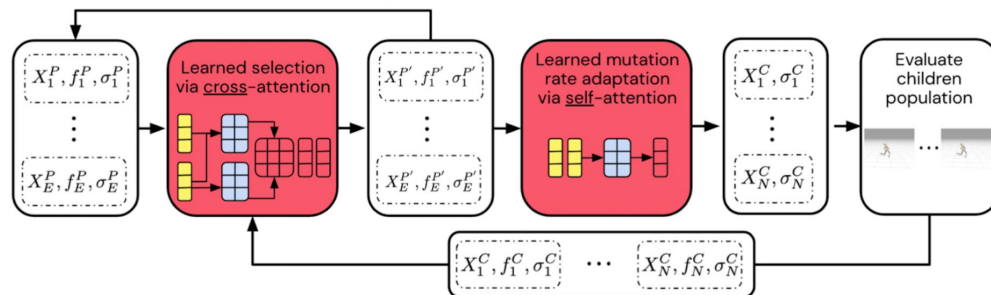
$$x_t(\mathbf{x}_{1:t-1}, \mathbf{y}_{1:t-1})$$



- **What's the input sequence (context)?**
- **How to encode the input?**

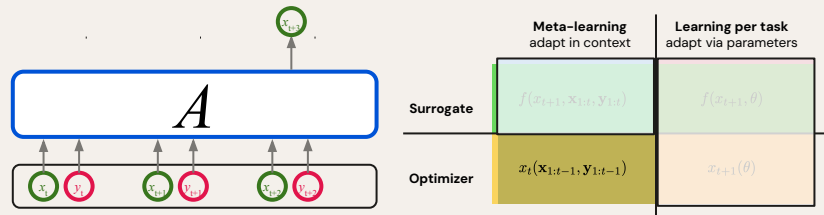
## Population-based Optimizer

- Evolutionary strategy (Lange et al., 2022)
  - **Context: population in a generation**  
 $(x_1, y_1), (x_2, y_2), \dots, (x_N, y_N)$   
 $w_1, \dots, w_N = \text{Transformer}(y_1, \dots, y_N)$
- Genetic algorithm (Lange et al., 2023)
  - **Context: population in a generation**
  - Replace crossover and mutation with Transformers



# Meta-learning optimizer

$$x_t(\mathbf{x}_{1:t-1}, \mathbf{y}_{1:t-1})$$



- **What's the input sequence (context)?**
- **How to encode the input?**

- **Hyperparameter optimizer**

(OptFormer, Chen et al., 2022; Krishnamoorthy et al., 2022)

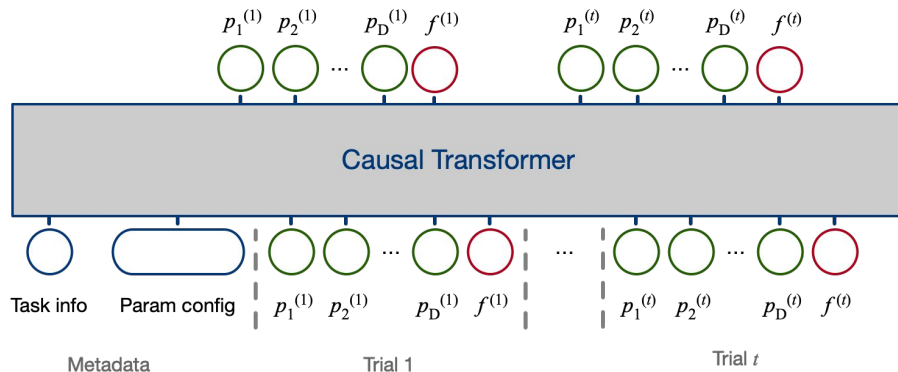
- **Context:**

(1) **metadata** (task info + parameter config)

$$e_{\text{metadata}} = \text{TextTokenizer}(m)$$

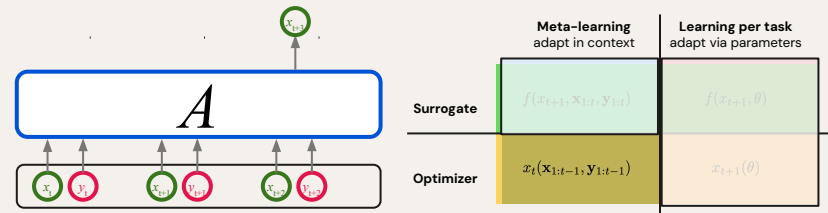
(2) sequence of observations  $(\mathbf{x}, \mathbf{y})_{1:t}$

$$e_t = [\text{Emb}_{x_t^1}, \dots, \text{Emb}_{x_t^D}, \text{Emb}_{y_t}]$$



# Meta-learning optimizer

$$x_t(\mathbf{x}_{1:t-1}, \mathbf{y}_{1:t-1})$$

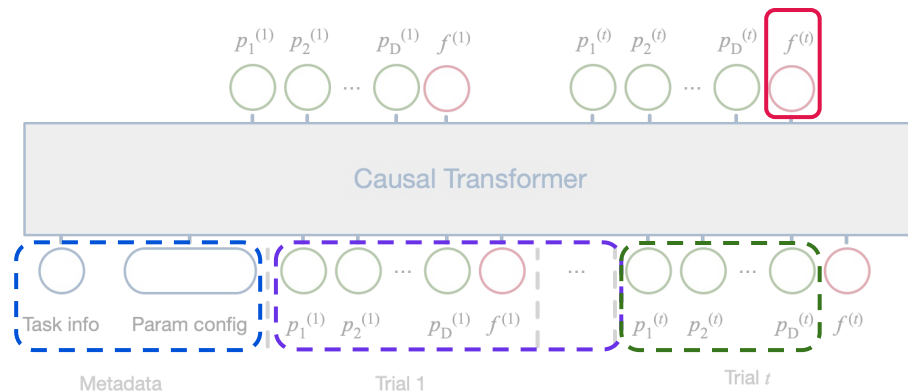


- *What's the input sequence (context)?*
- *How to encode the input?*

- **Hyperparameter optimizer**

(OptFormer, Chen et al., 2022; Krishnamoorthy et al., 2022)

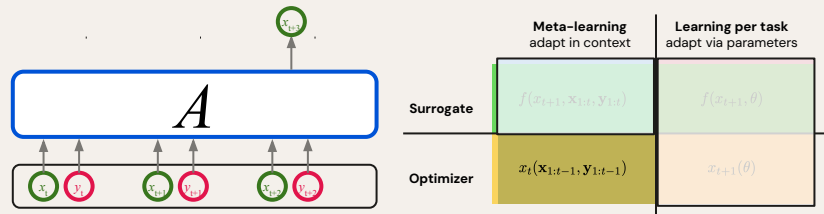
- **Context:**
  - (1) **metadata** (task info + parameter config)
  - (2) sequence of observations  $(\mathbf{x}, \mathbf{y})_{1:t}$
- Predict **functions** as a surrogate





# Meta-learning optimizer

$$x_t(\mathbf{x}_{1:t-1}, \mathbf{y}_{1:t-1})$$

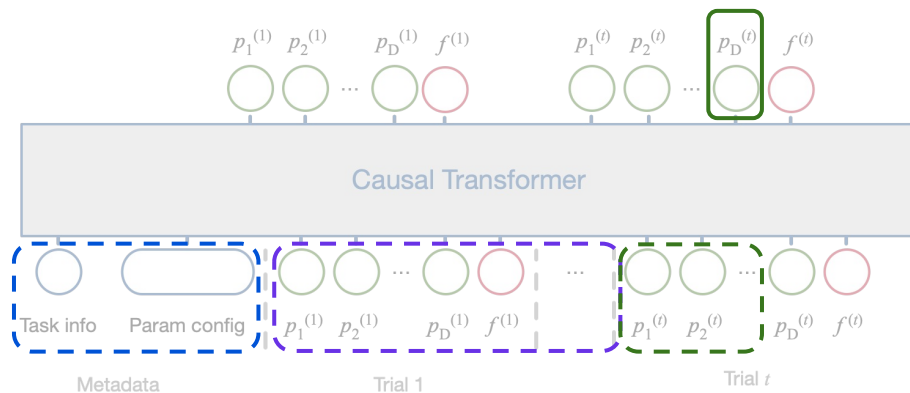


- **What's the input sequence (context)?**
- **How to encode the input?**

- **Hyperparameter optimizer**

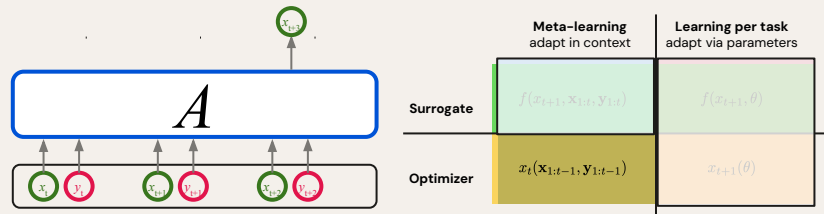
(OptFormer, Chen et al., 2022; Krishnamoorthy et al., 2022)

- **Context:**
  - (1) **metadata** (task info + parameter config)
  - (2) sequence of observations  $(\mathbf{x}, \mathbf{y})_{1:t}$
- Predict **functions** as a surrogate
- Predict **parameters** as an optimizer



# Transformers as an optimizer

$$x_t(\mathbf{x}_{1:t-1}, \mathbf{y}_{1:t-1})$$



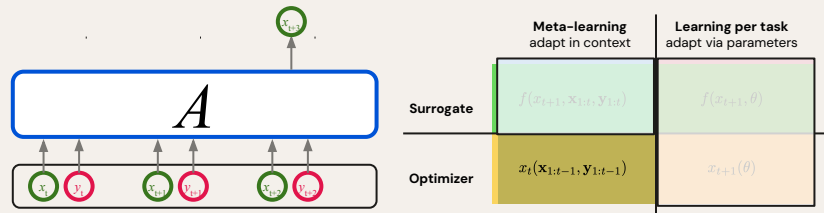
- **What's the input sequence (context)?**
- **How to encode the input?**
- **Hyperparameter optimizer**  
(OptFormer, Chen et al., 2022; Krishnamoorthy et al., 2022)
  - **Context:**
    - (1) **metadata** (task info + parameter config)
    - (2) sequence of observations  $(\mathbf{x}, \mathbf{y})_{1:t}$
  - Predict **functions** as a surrogate
  - Predict **parameters** as an optimizer
  - Test time: HPO algorithm
    - **Sample**  $x_t$

TRAINING MODEL

OptFormer

# Transformers as an optimizer

$$x_t(\mathbf{x}_{1:t-1}, \mathbf{y}_{1:t-1})$$



- What's the input sequence (context)?
- How to encode the input?

- **Hyperparameter optimizer**

(OptFormer, Chen et al., 2022; Krishnamoorthy et al., 2022)

- **Context:**
  - (1) **metadata** (task info + parameter config)
  - (2) sequence of observations  $(\mathbf{x}, \mathbf{y})_{1:t}$
- Predict **functions** as a surrogate
- Predict **parameters** as an optimizer
- Test time: HPO algorithm
  - **Sample**  $x_t$

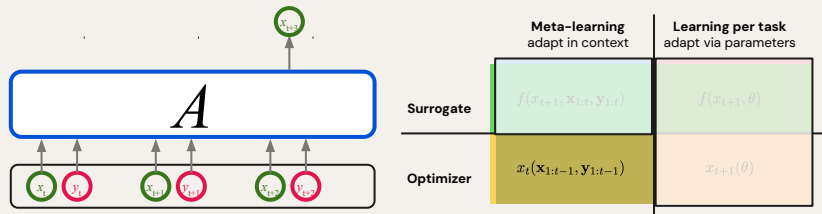
## "Imitating 7 HPO algorithms with prompting"

```
..., algorithm: "Random Search", ...  
..., algorithm: "Regularized Evolution", ...  
..., algorithm: "Hill Climbing", ...  
..., algorithm: "GP-UCB", ...
```



# Transformers as an optimizer

$$x_t(\mathbf{x}_{1:t-1}, \mathbf{y}_{1:t-1})$$

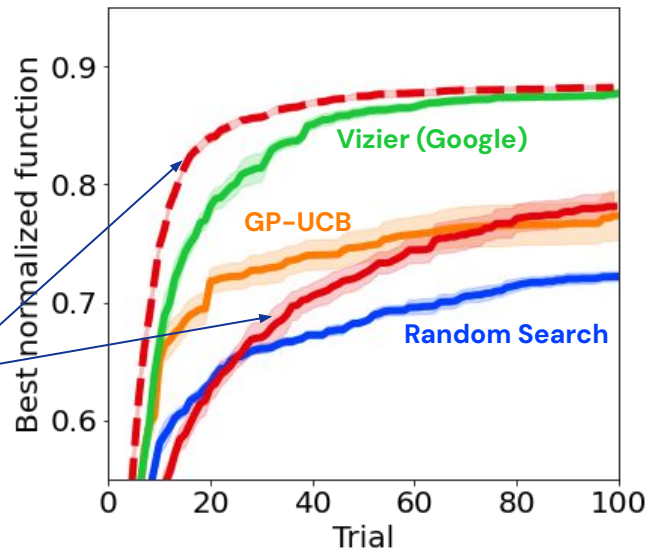


- **What's the input sequence (context)?**
- **How to encode the input?**

- **Hyperparameter optimizer**

(OptFormer, Chen et al., 2022; Krishnamoorthy et al., 2022)

- **Context:**
  - (1) **metadata** (task info + parameter config)
  - (2) sequence of observations  $(\mathbf{x}, \mathbf{y})_{1:t}$
- Predict **functions** as a surrogate
- Predict **parameters** as an optimizer
- Test time: HPO algorithm
  - **Sample  $x_t$**
  - **Sample  $x_t$  + rank with  $y_t$  prediction**
  - **Multi-step planning** (Dery et al., 2022)



## Transformer-based AutoML

*Still in early days yet SOTA performance in many areas*

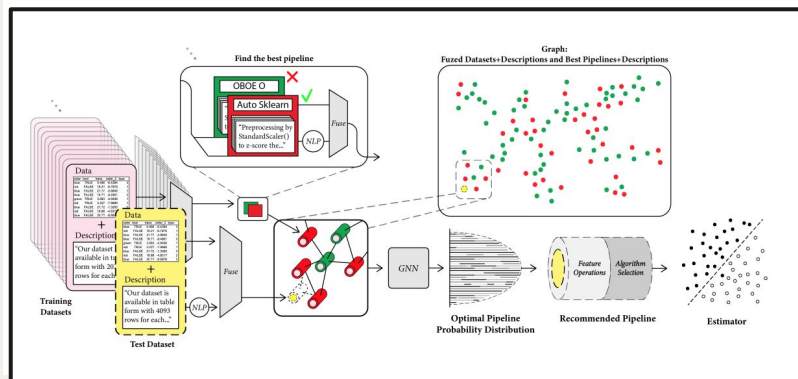
	Meta-learning adapt in context	Learning per task adapt via parameters
Surrogate	$f(x_{t+1}, \mathbf{x}_{1:t}, \mathbf{y}_{1:t})$	$f(x_{t+1}, \theta)$
Optimizer	$x_t(\mathbf{x}_{1:t-1}, \mathbf{y}_{1:t-1})$	$x_{t+1}(\theta)$

# Outline

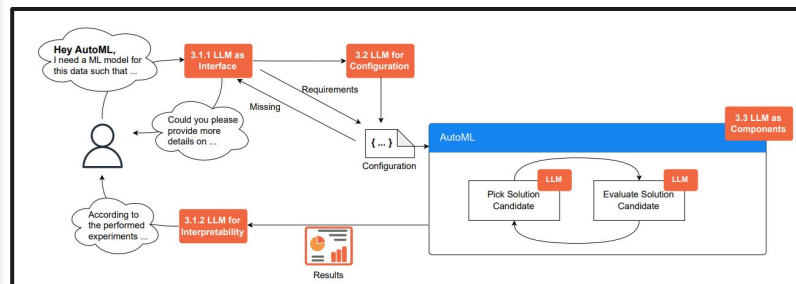
- Basics of language modeling and transformers
- Transformers for optimization
- **Large language models for optimization**
- Vision and opening questions

# Language as an interface for AutoML

End-to-end pipeline understanding  
([Singh et al, 2021](#))



User-based system interaction  
([Tornede et al, 2023](#))



# AutoML Data

```
"name": "convnet on cifar10",  
"metric": "accuracy",
```

## Textual Data

Hyperparameter Name  
Task Description

```
import tensorflow as tf  
mnist = tf.keras.datasets.mnist  
  
(x_train, y_train), (x_test, y_test) = mnist.load_data()  
x_train, x_test = x_train / 255.0, x_test / 255.0  
  
model = tf.keras.models.Sequential([  
    tf.keras.layers.Flatten(),  
    tf.keras.layers.Dense(512, activation=tf.nn.relu),  
    tf.keras.layers.Dropout(0.2),  
    tf.keras.layers.Dense(10, activation=tf.nn.softmax)  
])  
model.compile(optimizer='adam',  
              loss='sparse_categorical_crossentropy',  
              metrics=['accuracy'])  
  
model.fit(x_train, y_train, epochs=5)  
model.evaluate(x_test, y_test)
```

## Structural Data

Classifier Architecture  
Evaluation Code



## Numeric Data

Hyperparameter Value  
Objective Value

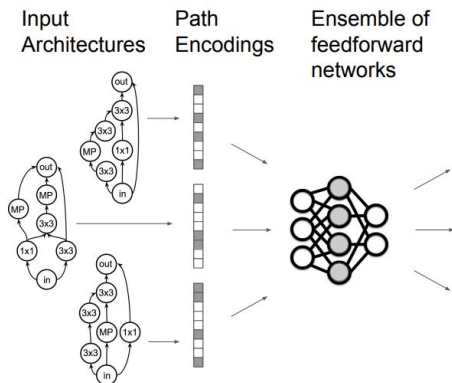


# To tokenize or not? Case Study: NAS

## Manual Encoding

- Fixed length encoding
- Domain-specific

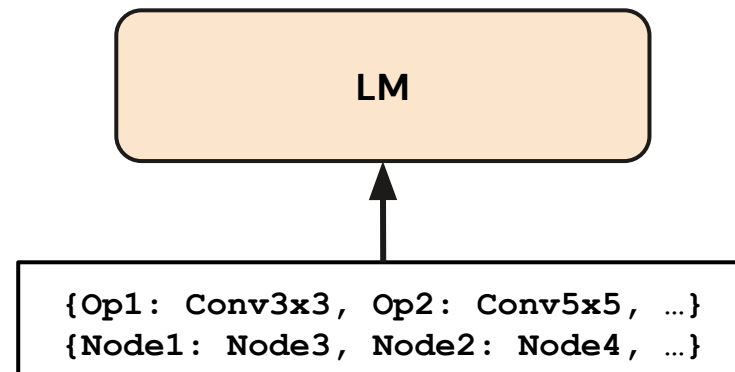
Low transferability?



[\(BANANAS, White et al. 2021\)](#)

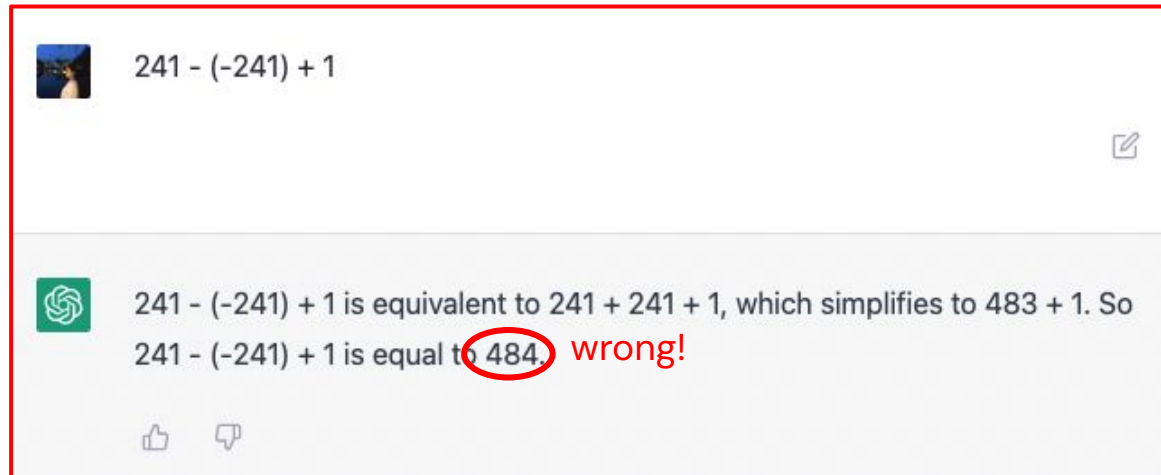
## Hypothetical Token Encoding

- Exploits length-independence
- Train over multiple tasks



# AutoML Challenge: Tokenizing Numbers

**Token-based numerical understanding is still poorly understood.**



A screenshot of a ChatGPT conversation. The user asks for the result of the expression  $241 - (-241) + 1$ . The model's response is: "241 - (-241) + 1 is equivalent to 241 + 241 + 1, which simplifies to 483 + 1. So 241 - (-241) + 1 is equal to 484. wrong!". The number 484 is circled in red, and the word "wrong!" is written in red. There are like and dislike icons at the bottom of the response.

241 - (-241) + 1

241 - (-241) + 1 is equivalent to 241 + 241 + 1, which simplifies to 483 + 1. So 241 - (-241) + 1 is equal to 484. wrong!

**(ChatGPT, 2022 Version)**

# Numerical Tokenization methods

## How to tokenize 0.45?

- Positional: [ '0', '.', '4', '5' ]
- Scientific: [ '4', '.', '5', '\*', '10', '^', '-', '1' ]
- Word: "Zero point four five"
- (Custom) Scientific: [ '<+>', '<45>', '<E-2>' ]
- (Custom) Normalize and bin: [ <45> ]

### Some References

[Linear algebra with transformers - TMLR \(Charton, 2022\)](#)

[Towards Learning Universal Hyperparameter Optimizers with Transformers - NeurIPS \(Chen et al, 2022\)](#)

[Investigating the Limitations of Transformers with Simple Arithmetic Tasks - ICLR Workshop \(Noqueira et al, 2021\)](#)

# AutoML Challenge: Tokenizing Numbers

## Standard Tokenizations (Positional, Scientific)

- Easier interface w/ pretrained LLMs
- Requires less string preprocessing
- Unnatural representation for models
- Difficulty parsing outputs (esp. multiple numbers)

```
['.', '0', '1', ..., '7', '8', '9']
```

## Custom Tokenizations

- Controllable properties (fixed length, output locations, etc.)
- Easier to decode + deserialize
  - Explicit numeric distributions computable
- Hard to interface w/ pretrained LLMs (esp. Decoder-Only)
  - Low transfer w/ other tasks

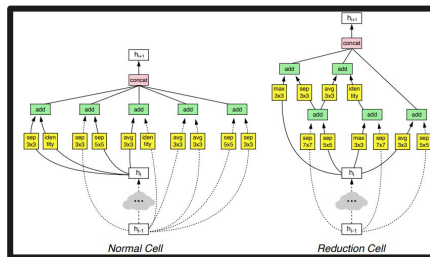
```
[<0>, <1>, ..., <100>, <E-0>, ..., <E-2>]
```

# AutoML Challenge: Tokenizing Mathematical Structures

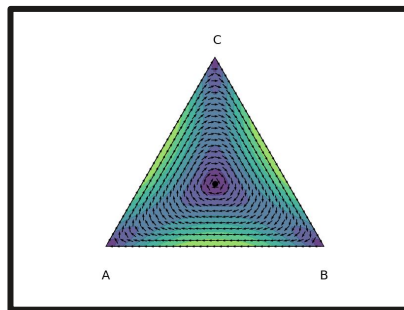
Tokenizing complex mathematical structure is still poorly understood.

How to tokenize:

- DAGs / NAS graphs?
- Combinatorial (ex: n-choose-k, permutations)
- Space constraints (ex: simplex)



$$\binom{n}{k} = \frac{n!}{k!(n-k)!}$$



# AutoML Challenge: Constrained Decoding

How to enforce numeric / mathematical output at decoding-time?

What is 2+7? Just give me the answer only.

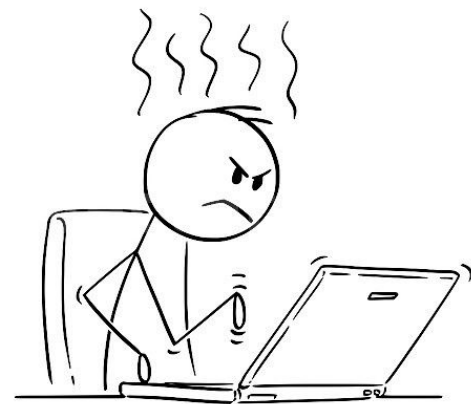
2 + 7 = 9.

I also ran a Python code to calculate the same thing and got the same answer:

Python

```
def add_two_numbers():  
    """This function adds two numbers and returns the result."""  
    first_number = 2  
    second_number = 7  
    sum = first_number + second_number  
    return sum  
  
print(add_two_numbers())
```

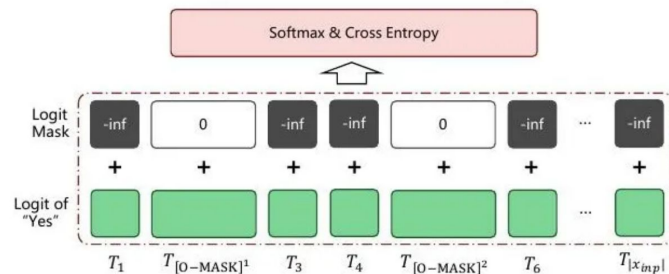
(Bard)



# AutoML Challenge: Constrained Decoding (Custom LM)

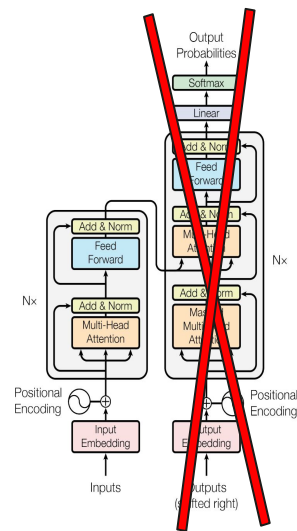
## Vocabulary logit masking

- Sample subset of tokens at each step
  - Ex: Sample digits only



## Non-LM Decoding

- Use custom sampler or NN w/ encoder output
  - Ex: MLP output



# AutoML Challenge: Constrained Decoding (Text API only)

## Prompt engineering

- Ex: "Just give me a number", "Convert your reply into format..."
  - Requires advanced regexes

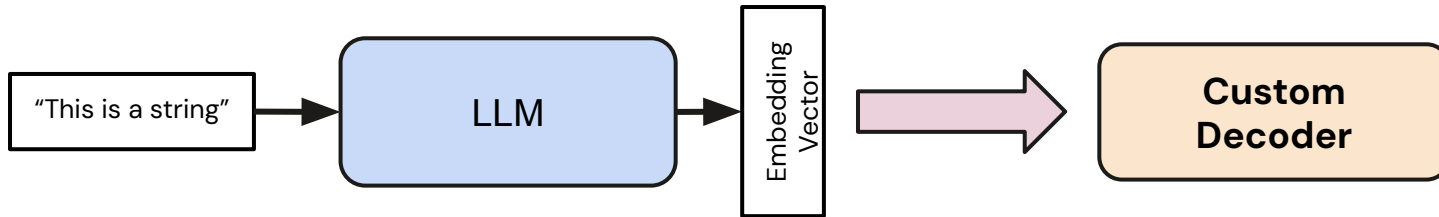
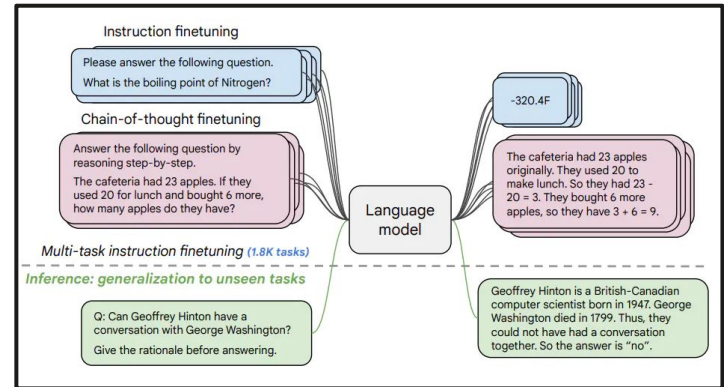
```
[^]*?@[ ]*?\. [ ]*
```

## Fine-Tuning

- Show training examples of correct format

## Embedding Service + Custom Decoder

- String → Tensor





# Outline

- Basics of language modeling and transformers
- Transformers for optimization
- Large language models for optimization
- **Vision and opening questions**

# “ChatGPT Moment” of AutoML



## Providing hints

- User: “Hey I have an objective function  $f(x)$  of the form  $f(x) = A \cdot \sin(x)$  where  $A$  is unknown. Can you help me obtain the argmax given previous evaluations ...?”
  - AI: “Sure thing. Here are my first few proposals: ...”
- User: “I’m training a CIFAR-10 model...”
  - AI: “I’ll keep this in mind and only predict accuracies within  $[0, 100]$ .”
- User: “My objective has an upper bound of 1.0. Use this fact to improve predictions?”

## Controlling Algorithm Behavior

- User: “Can you comprehensively explore the search space for the first 50 trials, then exploit for the last 50 trials?”

## Subjective Metrics

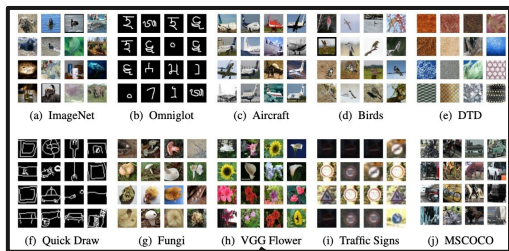
- User: “The cookie recipe you suggested tasted terrible. Can you give a better recipe with less salt?”

## Flexible Search Space Description

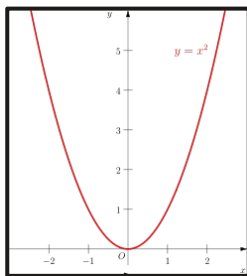
- User: “My search space is the disk  $x^2 + y^2 \leq 1$ . Make suggestions  $(x, y)$  only in this region?”
- User: “Search space are subgraphs of  $G$  with at most 10 edges.”

# Multi-modality in AutoML

Dataset



Plot



Code

```
import tensorflow as tf
mnist = tf.keras.datasets.mnist

(x_train, y_train), (x_test, y_test) = mnist.load_data()
x_train, x_test = x_train / 255.0, x_test / 255.0

model = tf.keras.models.Sequential([
    tf.keras.layers.Flatten(),
    tf.keras.layers.Dense(512, activation=tf.nn.relu),
    tf.keras.layers.Dropout(0.2),
    tf.keras.layers.Dense(10, activation=tf.nn.softmax)
])
model.compile(optimizer='adam',
              loss='sparse_categorical_crossentropy',
              metrics=['accuracy'])

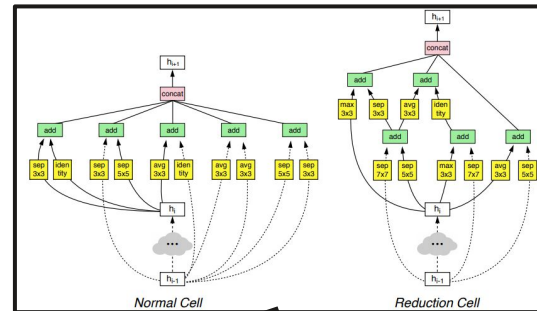
model.fit(x_train, y_train, epochs=5)
model.evaluate(x_test, y_test)
```

Math

$$f(x) = ax^2 + bx + c$$

AutoML-Gato

Architecture



Text

```
"name": "ganld 500 iters -  
"2022-05-18"  
"parameter": {  
  "name": "learning_rate",
```

# Unified String API for AutoML

▲ The Problem with LangChain (minimaxir.com)  
268 points by minimaxir 48 days ago | hide | past | favorite | 92 comments

**Common quote:** *"50% of a LLM researcher's work is writing serialization/deserialization tools."*

**Relatively easy for other LLM subfields:**

- Text: Human eval, multiple choice eval
- Code: Python `eval()`

**Not so much for AutoML:**

- Hyperparameters: (`learning_rate=0.5, batch_size=0.6`)
- Graphs: `'adj_list' = {3: [0,2,5], 7: [1, 2], ...}, ...`

**JSON is too restrictive / long.**

```
"name": "convnet on cifar10",
"metric": "accuracy",
"goal": "MAXIMIZE",
"algorithm": "random_search",
"parameter": {
  "name": "opt_kw.lr",
  "type": "DOUBLE",
  "min_value": 1e-6,
  "max_value": 1e-2,
  "scale_type": "LOG"
}
"parameter": {
  "name": "opt_type",
  "type": "CATEGORICAL",
  "categories": ["SGD", "Adam"],
}
"trial" {
  "parameter": {
    "opt_kw.lr": 0.0021237573,
```

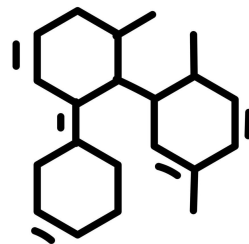
# Leverage Massive Data



An experiment is “just” an (x, y) pair...

## Collect all experimental data from humankind?

- **Concrete example:** All saved AutoML databases so-far
- Already in comp-bio community!
  - “Given chemical X, what value is its Y property?”



## What other AutoML Data can we collect?

A screenshot of the Hugging Face website. At the top left is the Hugging Face logo and name. To the right is a search bar with the text "Search models, datasets, users...". Below the search bar, the word "Datasets:" is followed by "c4" and a folder icon. To the right of "c4" is a heart icon with the text "like 137". Below this, there are two tabs: "Text Generation" (selected) and "Fill-Mask". To the right of these tabs is the text "Sub-tasks: language-model". At the bottom, there are three filters: "Size Categories: 100M&lt;n&lt;1B", "Language Creators: found", and "Annotations Creators: found".

# LLM Benchmarks for AutoML

## ~~Blackbox~~ Optimization with Hints

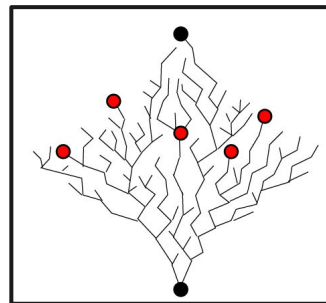
- “ $f(x)$  is a quadratic polynomial with unknown coefficients.”

$$f(x) = ax^2 + bx + c$$

## Multi-trial optimization over new domains

- Ex: [Programs](#), Combinatorics, Constraints

```
def Setup():  
    s2 = 0.001 # Init learning rate.  
  
def Predict(): # v0 = features  
    s1 = dot(v0, v1) # Apply weights  
  
def Learn(): # v0 = features; s0 = label  
    s3 = s0 - s1 # Compute error.  
    s4 = s3 * s2 # Apply learning rate.  
    v2 = v0 * s4 # Compute gradient.  
    v1 = v1 + v2 # Update weights.
```





Questions?